call INSERT $R$, \#S (P : X 1471/500 :Y 139/200)
structure view:

data view:

call CHOOSE-LEAF $R, 0$
a leaf is found: root return from CHOOSE-LEAF
the leaf root is not full, add the record.

call ADJUST-TREE with $R$, node root
we are at the root
return from ADJUST-TREE
call INSERT $R$, \#S (P : X 467/1000 :Y 33/500)
structure view:

| 0 |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- |

data view:

call CHOOSE-LEAF $R, 1$
a leaf is found: root
return from CHOOSE-LEAF
the leaf root is not full, add the record.

call ADJUST-TREE with $R$, node root we are at the root
return from ADJUST-TREE
call INSERT $R$, \#S (P : X 1123/500 : Y 579/500)
structure view:

| 0 | 1 |  |  |  |
| :--- | :--- | :--- | :--- | :--- |

data view:

call CHOOSE-LEAF $R, 2$
a leaf is found: root
return from CHOOSE-LEAF
the leaf root is not full, add the record.

$$
\begin{array}{|l|l|l|l|l}
\hline 0 & 1 & & & \\
\hline
\end{array} \quad \rightarrow \quad \rightarrow \quad \begin{array}{|l|l|l|l|l|}
\hline 0 & 1 & 2 & & \\
\hline
\end{array}
$$

call ADJUST-TREE with $R$, node root we are at the root return from ADJUST-TREE
call INSERT $R$, \#S (P : X 1161/1000 : Y 89/200)
structure view:

$$
\begin{array}{|l|l|l|l|l|}
\hline 0 & 1 & 2 & & \\
\hline
\end{array}
$$

data view:

call CHOOSE-LEAF $R, 3$
a leaf is found: root
return from CHOOSE-LEAF
the leaf root is not full, add the record.

$$
\begin{array}{|l|l|l|l|l}
\hline 0 & 1 & 2 & & \\
\hline
\end{array} \quad \rightarrow \quad \rightarrow \quad \begin{array}{|l|l|l|l|l|}
\hline 0 & 1 & 2 & 3 & \\
\hline
\end{array}
$$

call ADJUST-TREE with $R$, node root we are at the root return from ADJUST-TREE
call INSERT $R$, \#S (P : X 1943/500 :Y 121/1000)
structure view:

$$
\begin{array}{|l|l|l|l|l|}
\hline 0 & 1 & 2 & 3 & \\
\hline
\end{array}
$$

data view:

call CHOOSE-LEAF $R, 4$
a leaf is found: root
return from CHOOSE-LEAF
the leaf root is not full, add the record.

$$
\begin{array}{|l|l|l|l|l}
\hline 0 & 1 & 2 & 3 & \\
\hline
\end{array} \quad \longrightarrow \quad \begin{array}{|l|l|l|l|l|}
\hline 0 & 1 & 2 & 3 & 4 \\
\hline
\end{array}
$$

call ADJUST-TREE with $R$, node root we are at the root
return from ADJUST-TREE
call INSERT $R$, \#S (P : X 1153/500 :Y 2403/1000)
structure view:

$$
\begin{array}{|l|l|l|l|l|}
\hline 0 & 1 & 2 & 3 & 4 \\
\hline
\end{array}
$$

data view:

call CHOOSE-LEAF $R, 5$
a leaf is found: root
return from CHOOSE-LEAF
call SPLIT-NODE $R$ new node
call PICK-SEEDS

separation $=0.88947225$
axis $y$

separation $=0.8423335$
call PICK-NEXT $R$ entries node

$0: \Delta d=-0.6224873$
maximal $|\Delta d|$ is for node 0 .
add the node to the red group $(\Delta d<0)$
update MBR of the red group group
call PICK-NEXT $R$ entries node


2: $\Delta d=-2.4023884$
maximal $|\Delta d|$ is for node 2.
add the node to the red group $(\Delta d<0)$ update MBR of the red group group
call PICK-NEXT $R$ entries node


3: $\Delta d=2.0878043$
maximal $|\Delta d|$ occurs for node 3.
add the node to the blue group ( $\Delta d \geq 0$ ) update MBR of the blue group group
call PICK-NEXT $R$ entries node


4: $\Delta d=1.2795372$
maximal $|\Delta d|$ occurs for node 4.
add the node to the blue group $(\Delta d \geq 0)$ update MBR of the blue group group
... the final split is:

call ADJUST-TREE with $R$, node A and the new node
we are at the root
return from ADJUST-TREE
call INSERT $R$, \#S (P : X 428/125 :Y 1207/500)
structure view:

data view:

call CHOOSE-LEAF $R, 6$
choose among children:

old area: 2.0954008
new area: 9.2212105
extension: 7.1258097
selected B
a leaf is found: B
return from CHOOSE-LEAF
the leaf B is not full, add the record.

$$
\begin{array}{|l|l|l|l|l}
\hline 0 & 2 & 5 & & \\
\hline
\end{array} \quad \rightarrow \quad \begin{array}{ll|l|l|l|l|}
\hline 0 & 2 & 5 & 6 & \\
\hline
\end{array}
$$

call ADJUST-TREE with $R$, node B update MBR of node B .
continue by adjusting the parent node root
call ADJUST-TREE with $R$, node root we are at the root return from ADJUST-TREE
call INSERT $R$, \#S (P : X 53/125 :Y 2153/1000)
structure view:

data view:

call CHOOSE-LEAF $R, 7$
choose among children:

old area: 2.0954008
new area: 8.374993
extension: 6.2795925
selected B
a leaf is found: B
return from CHOOSE-LEAF
the leaf B is not full, add the record.

$$
\begin{array}{|l|l|l|l|l|}
\hline 0 & 2 & 5 & 6 & \\
\hline
\end{array} \quad \rightarrow \quad \begin{array}{|l|l|l|l|l|}
\hline 0 & 2 & 5 & 6 & 7 \\
\hline
\end{array}
$$

call ADJUST-TREE with $R$, node B update MBR of node B .
continue by adjusting the parent node root
call ADJUST-TREE with $R$, node root we are at the root return from ADJUST-TREE
call INSERT $R$, \#S (P : X 1923/1000 :Y 1693/500)
structure view:

data view:

call CHOOSE-LEAF $R, 8$
choose among children:

old area: 2.0954008
new area: 12.738878
extension: 10.643477

old area: 6.1407995
new area: 9.251199
extension: 3.1103993
selected B
a leaf is found: B
return from CHOOSE-LEAF
call SPLIT-NODE $R$ new node
call PICK-SEEDS
axis $x$

separation $=0.8750001$
axis $y$

separation $=0.8616396$
call PICK-NEXT $R$ entries node


2: $\Delta d=0.6757961$
maximal $|\Delta d|$ occurs for node 2.
add the node to the blue group $(\Delta d \geq 0)$
update MBR of the blue group group
call PICK-NEXT $R$ entries node


5: $\Delta d=-0.4658308$
maximal $|\Delta d|$ is for node 5 .
add the node to the red group $(\Delta d<0)$
update MBR of the red group group
call PICK-NEXT $R$ entries node


6: $\Delta d=-0.72774005$
maximal $|\Delta d|$ is for node 6.
add the node to the red group $(\Delta d<0)$
update MBR of the red group group
call PICK-NEXT $R$ entries node

$7: \Delta d=-1.3390801$
maximal $|\Delta d|$ is for node 7.
add the node to the red group $(\Delta d<0)$
update MBR of the red group group
the rest of rectangles must be put to the blue group.
... the final split is:

call ADJUST-TREE with $R$, node B and the new node update MBR of node B.
add the new node to the parent node root
call ADJUST-TREE with $R$, node root
we are at the root
return from ADJUST-TREE
call INSERT $R$, \#S (P : X 51/500 :Y 3731/1000)
structure view:

data view:

call CHOOSE-LEAF $R, 9$
choose among children:

old area: 2.0954008
new area: 15.398158
extension: 13.302757 selected B
a leaf is found: B return from CHOOSE-LEAF
the leaf B is not full, add the record.

$$
\begin{array}{|l|l|l|l|l}
\hline 5 & 6 & 7 & 8 & \\
\hline
\end{array} \quad \longrightarrow \quad \longrightarrow \quad \begin{array}{|l|l|l|l|l|}
\hline 5 & 6 & 7 & 8 & 9 \\
\hline
\end{array}
$$

call ADJUST-TREE with $R$, node B update MBR of node B .
continue by adjusting the parent node root
call ADJUST-TREE with $R$, node root we are at the root return from ADJUST-TREE
call INSERT $R$, \#S (P : X 1017/500 :Y 1171/1000)
structure view:

data view:

call CHOOSE-LEAF $R, 10$
choose among children:

old area: 2.0954008
new area: 4.722795
extension: 2.6273942
selected C
a leaf is found: C
return from CHOOSE-LEAF
the leaf C is not full, add the record.

call ADJUST-TREE with $R$, node C update MBR of node C.
continue by adjusting the parent node root
call ADJUST-TREE with $R$, node root we are at the root return from ADJUST-TREE
call INSERT $R$, \#S (P : X 3161/1000 :Y 543/200)
structure view:

data view:

call CHOOSE-LEAF $R, 11$
choose among children:

old area: 2.0954008
new area: 10.31053
extension: 8.215129
selected B
a leaf is found: B
return from CHOOSE-LEAF

old area: 6.2621145
new area: 6.2621145
extension: 0.0

old area: 0.749008
new area: 2.9459398
extension: 2.1969319
call SPLIT-NODE $R$ new node
call PICK-SEEDS
axis $x$

separation $=0.8864283$
axis $y$

separation $=0.7750283$
call PICK-NEXT $R$ entries node


11: $\Delta d=1.7249506$
maximal $|\Delta d|$ occurs for node 11.
add the node to the blue group ( $\Delta d \geq 0$ )
update MBR of the blue group group
call PICK-NEXT $R$ entries node


5: $\Delta d=3.6333108$
maximal $|\Delta d|$ occurs for node 5 .
add the node to the blue group $(\Delta d \geq 0)$
update MBR of the blue group group
call PICK-NEXT $R$ entries node


6: $\Delta d=5.1024666$
maximal $|\Delta d|$ occurs for node 6.
add the node to the blue group $(\Delta d \geq 0)$
update MBR of the blue group group
the rest of rectangles must be put to the red group group.
... the final split is:

call ADJUST-TREE with $R$, node B and the new node update MBR of node B.
add the new node to the parent node root
call ADJUST-TREE with $R$, node root
we are at the root
return from ADJUST-TREE
call INSERT $R$, \#S (P : X 3801/1000 :Y 9/200)
structure view:

data view:

call CHOOSE-LEAF $R, 12$
choose among children:

old area: 2.0954008
new area: 2.1713999
extension: 0.07599902
selected A
a leaf is found: A
return from CHOOSE-LEAF
the leaf A is not full, add the record.

$$
\begin{array}{|l|l|l|l|l}
\hline 1 & 3 & 4 & & \\
\hline
\end{array} \quad \longrightarrow \quad \begin{array}{|l|l|l|l|l|}
\hline 1 & 3 & 4 & 12 & \\
\hline
\end{array}
$$

call ADJUST-TREE with $R$, node A update MBR of node A.
continue by adjusting the parent node root
call ADJUST-TREE with $R$, node root we are at the root return from ADJUST-TREE
call INSERT $R$, \#S (P : X 2749/1000 : Y 59/200)
structure view:

data view:

call CHOOSE-LEAF $R, 13$
choose among children:

old area: 2.1713999
new area: 2.1713999 extension: 0.0
selected A
a leaf is found: A
return from CHOOSE-LEAF
the leaf A is not full, add the record.

call ADJUST-TREE with $R$, node A update MBR of node A.
continue by adjusting the parent node root
call ADJUST-TREE with $R$, node root we are at the root return from ADJUST-TREE
call INSERT $R$, \#S (P : X 2 :Y 317/500)
structure view:

data view:

call CHOOSE-LEAF $R, 14$
choose among children:

old area: 2.1713999
new area: 2.8553908
extension: 0.68399096 selected C
a leaf is found: C
return from CHOOSE-LEAF
the leaf C is not full, add the record.

call ADJUST-TREE with $R$, node C update MBR of node C.
continue by adjusting the parent node root
call ADJUST-TREE with $R$, node root we are at the root return from ADJUST-TREE
call INSERT $R$, \#S (P : X 1413/500 :Y 831/1000)
structure view:

data view:

call CHOOSE-LEAF $R, 15$
choose among children:

old area: 2.1713999
new area: 3.5683337
extension: 1.3969338 selected C
a leaf is found: C
return from CHOOSE-LEAF

old area: 1.1014446
new area: 9.064399
extension: 7.962954

old area: 0.84165395
new area: 0.84165395
extension: 0.0

D

old area: 2.4383986 new area: 6.6687994 extension: 4.230401
the leaf C is not full, add the record.

$$
\begin{array}{|l|l|l|l|l|}
\hline 0 & 2 & 10 & 14 & \\
\hline
\end{array} \quad \rightarrow \quad \begin{array}{|l|l|l|l|l|}
\hline 0 & 2 & 10 & 14 & 15 \\
\hline
\end{array}
$$

call ADJUST-TREE with $R$, node C update MBR of node C.
continue by adjusting the parent node root
call ADJUST-TREE with $R$, node root we are at the root return from ADJUST-TREE
call INSERT $R$, \#S (P : X 2611/1000 : Y 1213/500)
structure view:

data view:

call CHOOSE-LEAF $R, 16$
choose among children:

old area: 2.1713999
new area: 9.340638
extension: 7.169238
selected D
a leaf is found: D
return from CHOOSE-LEAF
the leaf D is not full, add the record.

$$
\begin{array}{|l|l|l|l|l|}
\hline 5 & 6 & 7 & 11 & \\
\hline
\end{array} \quad \longrightarrow \quad \begin{array}{|l|l|l|l|l|}
\hline 5 & 6 & 7 & 11 & 16 \\
\hline
\end{array}
$$

call ADJUST-TREE with $R$, node D update MBR of node D.
continue by adjusting the parent node root
call ADJUST-TREE with $R$, node root we are at the root return from ADJUST-TREE
call INSERT $R$, \#S (P : X 1853/500 :Y 169/100)
structure view:

data view:

call CHOOSE-LEAF $R, 17$
choose among children:

old area: 2.1713999
new area: 6.6770544
extension: 4.5056543
selected C a leaf is found: C
return from CHOOSE-LEAF

old area: 1.1014446
new area: 8.524763
extension: 7.4233184

old area: 0.84165395 new area: 2.3939362 extension: 1.5522822

D

old area: 2.4383986 new area: 4.265449 extension: 1.8270505
call SPLIT-NODE $R$ new node
call PICK-SEEDS

separation $=0.7901366$
axis $y$

separation $=0.6815286$
call PICK-NEXT $R$ entries node

$0: \Delta d=0.8539182$
maximal $|\Delta d|$ occurs for node 0 .
add the node to the blue group $(\Delta d \geq 0)$
update MBR of the blue group group
call PICK-NEXT $R$ entries node


2: $\Delta d=0.6463742$
maximal $|\Delta d|$ occurs for node 2.
add the node to the blue group ( $\Delta d \geq 0$ )
update MBR of the blue group group
call PICK-NEXT $R$ entries node


10: $\Delta d=1.2911222$
maximal $|\Delta d|$ occurs for node 10.
add the node to the blue group $(\Delta d \geq 0)$
update MBR of the blue group group
the rest of rectangles must be put to the red group group.
... the final split is:

call ADJUST-TREE with $R$, node C and the new node update MBR of node C.
add the new node to the parent node root
call ADJUST-TREE with $R$, node root
we are at the root
return from ADJUST-TREE
call INSERT $R$, \#S (P : X 921/1000 : Y 7/200)
structure view:

data view:

| 9 |  | B |  |  |
| :---: | :---: | :---: | :---: | :---: |
|  | 7 |  | D 516 | [11) |
|  |  |  |  | 17 <br> C |
|  |  | $\begin{array}{r} 3 \\ -18 \\ \hline \end{array}$ | $\text { A } 13$ | 因 |

call CHOOSE-LEAF $R, 18$
choose among children:

old area: 2.1713999
new area: 2.2075899
extension: 0.036190033 selected A a leaf is found: A
return from CHOOSE-LEAF
call SPLIT-NODE $R$ new node call PICK-SEEDS

axis $y$

call PICK-NEXT $R$ entries node


1: $\Delta d=0.36655203$
maximal $|\Delta d|$ occurs for node 1.
add the node to the blue group ( $\Delta d \geq 0$ )
update MBR of the blue group group
call PICK-NEXT $R$ entries node


4: $\Delta d=0.60874004$
maximal $|\Delta d|$ occurs for node 4 .
add the node to the blue group ( $\Delta d \geq 0$ )
update MBR of the blue group group
call PICK-NEXT $R$ entries node


12: $\Delta d=1.6640002$
maximal $|\Delta d|$ occurs for node 12.
add the node to the blue group $(\Delta d \geq 0)$
update MBR of the blue group group
the rest of rectangles must be put to the red group group.
... the final split is:

call ADJUST-TREE with $R$, node A and the new node
update MBR of node A.
add the new node to the parent node root
Parent node root is full, promote split (create a new parent)
call SPLIT-NODE $R$ new node call PICK-SEEDS

separation $=0.17645586$

separation $=0.78670437$
call PICK-NEXT $R$ entries node


NIL: $\Delta d=-6.015692$
maximal $|\Delta d|$ is for node NIL.
add the node to the red group $(\Delta d<0)$ update MBR of the red group group
call PICK-NEXT $R$ entries node


NIL: $\Delta d=-12.085249$
maximal $|\Delta d|$ is for node NIL.
add the node to the red group $(\Delta d<0)$
update MBR of the red group group
call PICK-NEXT $R$ entries node


D: $\Delta d=-1.3273559$
maximal $|\Delta d|$ is for node D .
add the node to the red group $(\Delta d<0)$
update MBR of the red group group
the rest of rectangles must be put to the blue group.
...the final split is:

continue by adjusting the parent node NIL, the new parent
call ADJUST-TREE with $R$, node A and the new node we are at the root return from ADJUST-TREE
call INSERT $R$, \#S (P : X 3679/1000 : Y 283/250)
structure view:

data view:

call CHOOSE-LEAF $R, 19$
choose among children:

old area: 10.022879
new area: 12.452767
extension: 2.4298888
selected F
choose among children:

old area: 1.14372
new area: 1.14372 extension: 0.0 selected C
a leaf is found: C
return from CHOOSE-LEAF

D

old area: 2.4383986
new area: 6.1602645
extension: 3.721866

D

old area: 0.6258
new area: 2.8185659 extension: 2.1927657

E

old area: 1.035034
new area: 4.6938424
extension: 3.6588085
the leaf C is not full, add the record.

call ADJUST-TREE with $R$, node C
update MBR of node C.
continue by adjusting the parent node F
call ADJUST-TREE with $R$, node F update MBR of node F.
continue by adjusting the parent node root
call ADJUST-TREE with $R$, node root
we are at the root
return from ADJUST-TREE
call INSERT R, \#S (P : X 25/8 :Y 739/1000)
structure view:

data view:

call CHOOSE-LEAF $R, 20$
choose among children:

old area: 10.022879
new area: 10.62623
extension: 0.6033516
selected F
choose among children:

old area: 1.14372
new area: 1.2430799
extension: 0.09935987
selected C
a leaf is found: C
return from CHOOSE-LEAF

D

old area: 2.4383986
new area: 6.963199
extension: 4.5248003

D

old area: 0.6258
new area: 1.3936161
extension: 0.76781607

E

old area: 1.035034
new area: 3.271576
extension: 2.236542
the leaf C is not full, add the record.

call ADJUST-TREE with $R$, node C
update MBR of node C.
continue by adjusting the parent node F
call ADJUST-TREE with $R$, node F update MBR of node F.
continue by adjusting the parent node root
call ADJUST-TREE with $R$, node root
we are at the root
return from ADJUST-TREE
call INSERT $R$, \#S (P : X 877/250 : Y 319/125)
structure view:

data view:

call CHOOSE-LEAF $R, 21$
choose among children:

old area: 10.022879
new area: 11.888981
extension: 1.8661022
selected F
choose among children:

old area: 1.2430799
new area: 2.1740399
extension: 0.93095994 selected D
a leaf is found: D
return from CHOOSE-LEAF

old area: 2.4383986
new area: 2.5024066
extension: 0.064008

D

old area: 0.6258
new area: 6.257979
extension: 5.632179

old area: 1.035034
new area: 9.832822
extension: 8.797788
call SPLIT-NODE $R$ new node
call PICK-SEEDS

separation $=0.8781974$

separation $=0.47506586$
call PICK-NEXT $R$ entries node


21: $\Delta d=-1.7685543$
maximal $|\Delta d|$ is for node 21.
add the node to the red group $(\Delta d<0)$
update MBR of the red group group
call PICK-NEXT $R$ entries node


5: $\Delta d=-0.3776369$
maximal $|\Delta d|$ is for node 5 .
add the node to the red group $(\Delta d<0)$ update MBR of the red group group
call PICK-NEXT $R$ entries node


6: $\Delta d=-1.435199$
maximal $|\Delta d|$ is for node 6 .
add the node to the red group $(\Delta d<0)$
update MBR of the red group group
the rest of rectangles must be put to the blue group.
... the final split is:

call ADJUST-TREE with $R$, node G and the new node update MBR of node G.
add the new node to the parent node F
call ADJUST-TREE with $R$, node F
update MBR of node F.
continue by adjusting the parent node root
call ADJUST-TREE with $R$, node root
we are at the root
return from ADJUST-TREE
call INSERT $R$, \#S (P : X 21/100 :Y 2263/1000)
structure view:

data view:

call CHOOSE-LEAF $R, 22$
choose among children:

old area: 10.022879
new area: 10.022879 extension: 0.0
selected A
choose among children:

old area: 10.546558
new area: 11.162879
extension: 0.6163206

old area: 1.1014446
new area: 3.3710273
old area: 0.84165395
new area: 5.362628
extension: 4.520974
selected B
a leaf is found: B
return from CHOOSE-LEAF
the leaf B is not full, add the record.

call ADJUST-TREE with $R$, node B
update MBR of node $B$.
continue by adjusting the parent node A
call ADJUST-TREE with $R$, node A update MBR of node A.
continue by adjusting the parent node root
call ADJUST-TREE with $R$, node root
we are at the root
return from ADJUST-TREE
call INSERT $R$, \#S (P : X 147/50 : Y 283/250)
structure view:

data view:

call CHOOSE-LEAF $R, 23$
choose among children:

old area: 10.022879
new area: 10.022879 extension: 0.0
selected A
choose among children:

old area: 3.3710273
new area: 8.503361
extension: 5.1323338
old area: 0.84165395
new area: 0.84165395 extension: 0.0
selected E
a leaf is found: E
return from CHOOSE-LEAF
the leaf E is not full, add the record.

call ADJUST-TREE with $R$, node E
update MBR of node $E$.
continue by adjusting the parent node A
call ADJUST-TREE with $R$, node A update MBR of node A.
continue by adjusting the parent node root
call ADJUST-TREE with $R$, node root
we are at the root
return from ADJUST-TREE
call INSERT $R$, \#S (P : X 3737/1000 :Y 369/1000)
structure view:

data view:

call CHOOSE-LEAF $R, 24$
choose among children:

old area: 10.022879
new area: 13.660269
extension: 3.6373902
selected F
choose among children:

old area: 10.546558
new area: 10.546558
extension: 0.0

the leaf D is not full, add the record.

call ADJUST-TREE with $R$, node D
update MBR of node $D$.
continue by adjusting the parent node F
call ADJUST-TREE with $R$, node F update MBR of node F.
continue by adjusting the parent node root
call ADJUST-TREE with $R$, node root
we are at the root
return from ADJUST-TREE


