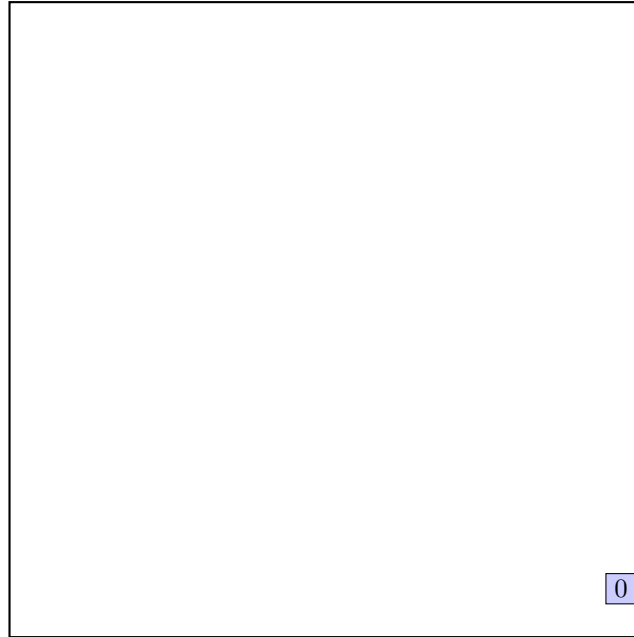


call INSERT R , #S(P :X 789/200 :Y 11/50)

structure view:



data view:

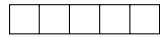


call CHOOSE-LEAF R , 0

a leaf is found: root

return from CHOOSE-LEAF

the leaf root is not full, add the record.



call ADJUST-TREE with R , node root

we are at the root

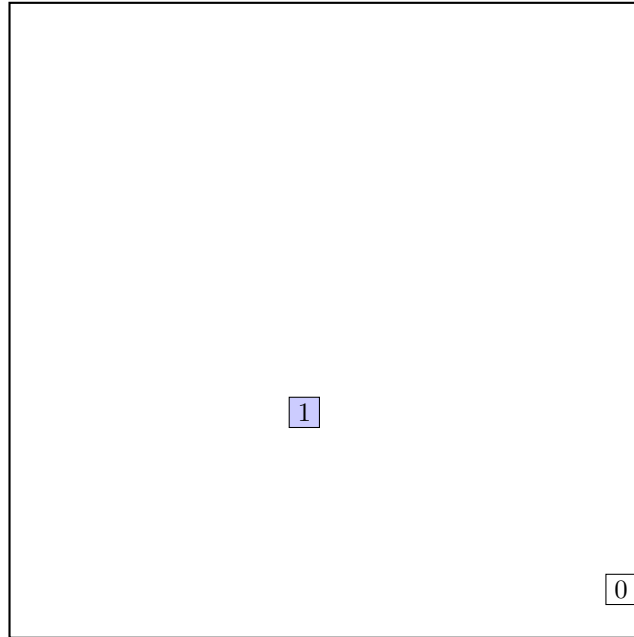
return from ADJUST-TREE

call INSERT R , #S(P :X 37/20 :Y 1391/1000)

structure view:



data view:

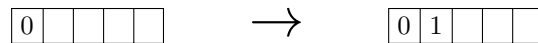


call CHOOSE-LEAF R , 1

a leaf is found: root

return from CHOOSE-LEAF

the leaf root is not full, add the record.



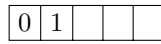
call ADJUST-TREE with R , node root

we are at the root

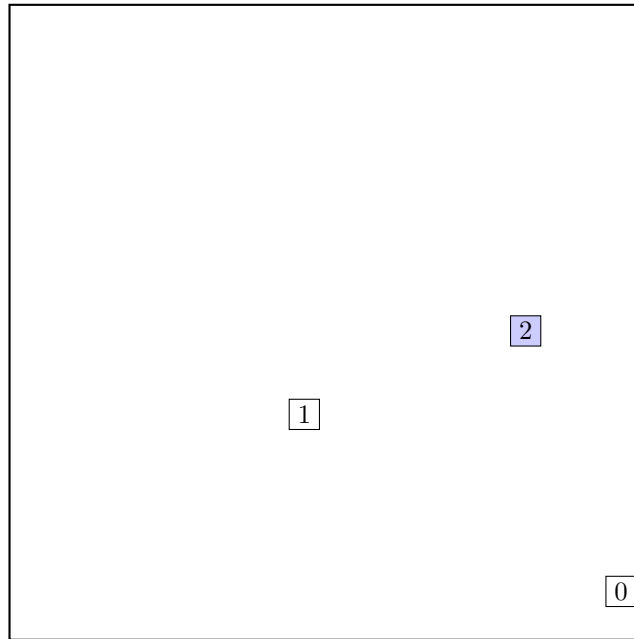
return from ADJUST-TREE

call INSERT R , #S(P :X 1657/500 :Y 1943/1000)

structure view:



data view:

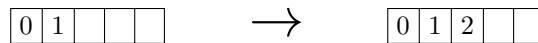


call CHOOSE-LEAF R , 2

a leaf is found: root

return from CHOOSE-LEAF

the leaf root is not full, add the record.



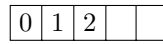
call ADJUST-TREE with R , node root

we are at the root

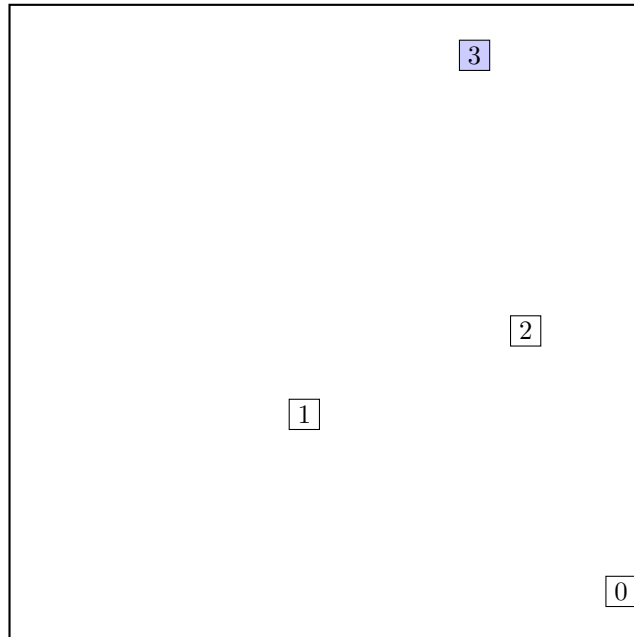
return from ADJUST-TREE

call INSERT R , #S(P :X 372/125 :Y 1883/500)

structure view:



data view:

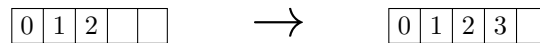


call CHOOSE-LEAF R , 3

a leaf is found: root

return from CHOOSE-LEAF

the leaf root is not full, add the record.



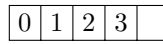
call ADJUST-TREE with R , node root

we are at the root

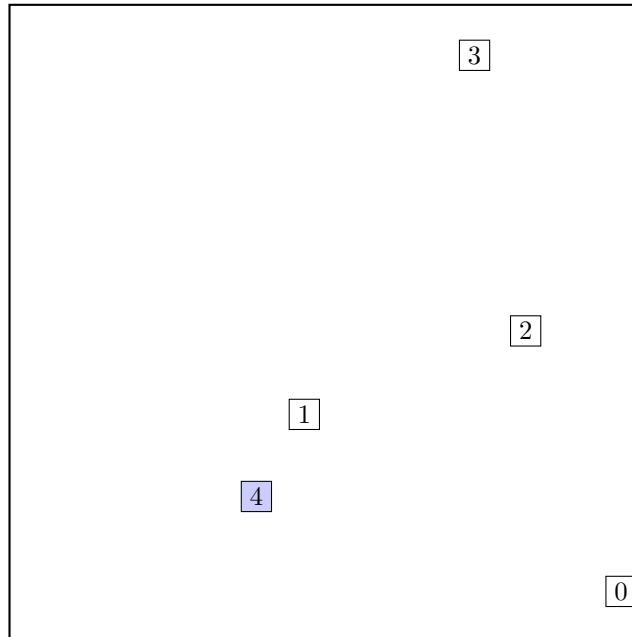
return from ADJUST-TREE

call INSERT R , #S(P :X 1533/1000 :Y 106/125)

structure view:



data view:

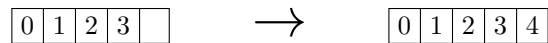


call CHOOSE-LEAF R , 4

a leaf is found: root

return from CHOOSE-LEAF

the leaf root is not full, add the record.



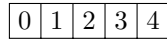
call ADJUST-TREE with R , node root

we are at the root

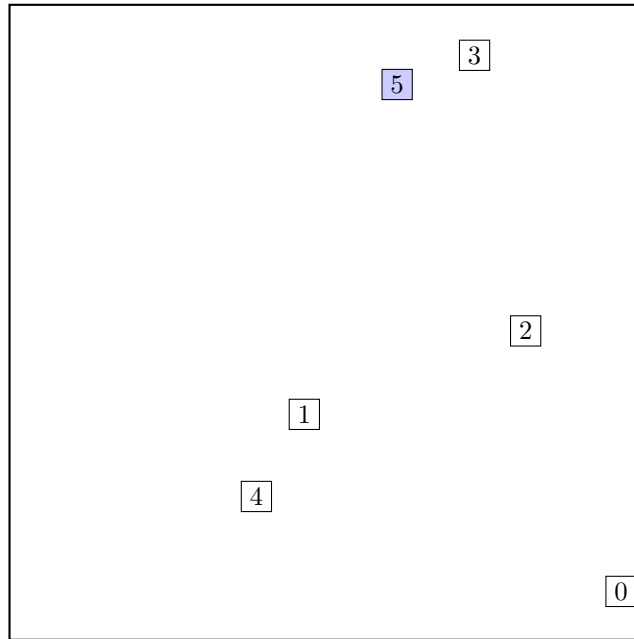
return from ADJUST-TREE

call INSERT R , #S(P :X 308/125 :Y 3573/1000)

structure view:



data view:



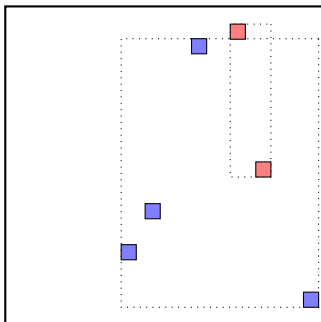
call CHOOSE-LEAF R , 5

a leaf is found: root

return from CHOOSE-LEAF

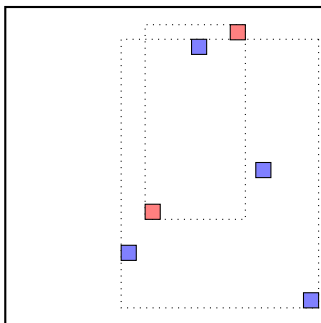
call SPLIT-NODE (bruteforce)

5 0 1 4 — 3 2



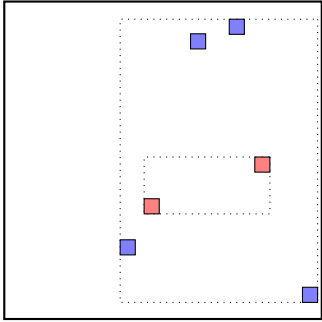
$S = 10.368809$

5 0 2 4 — 3 1



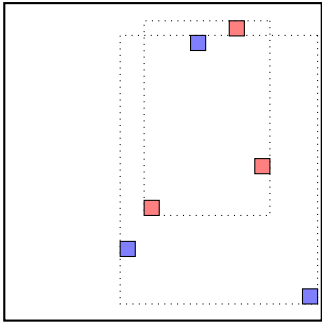
$S = 12.694885$

5 0 3 4 — 2 1



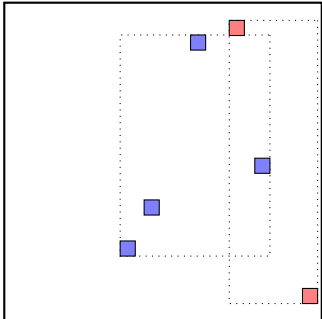
$S = 11.035879$

5 0 4 — 3 2 1



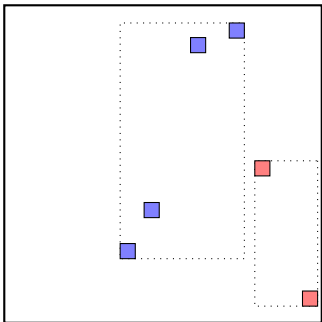
$S = 13.565235$

5 1 2 4 — 3 0



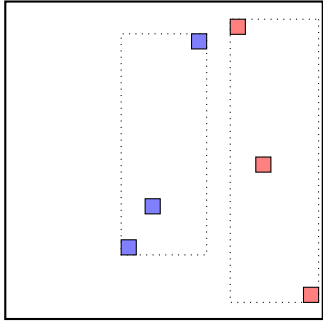
$S = 10.173498$

5 1 3 4 — 2 0



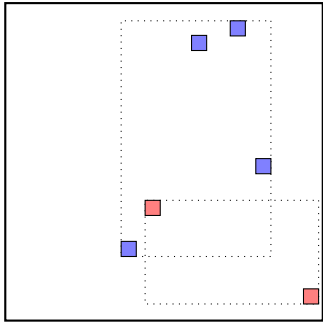
$S = 6.720887$

5 1 4 — 3 2 0



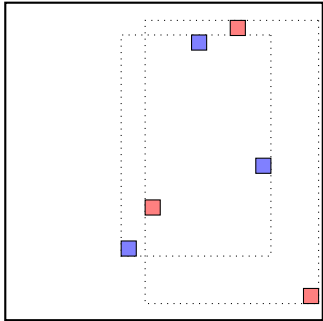
$S = 7.687248$

5 2 3 4 — 1 0



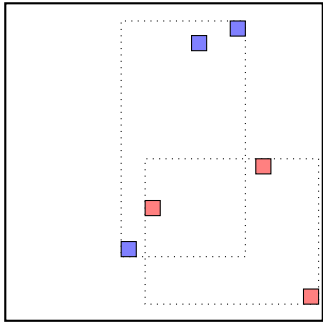
$S = 9.323202$

5 2 4 — 3 1 0



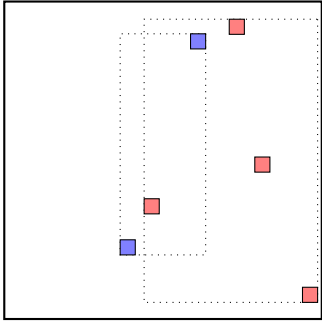
$S = 14.391495$

5 3 4 — 2 1 0



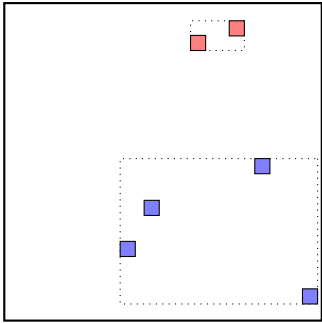
$S = 9.5361595$

5 4 — 3 2 1 0



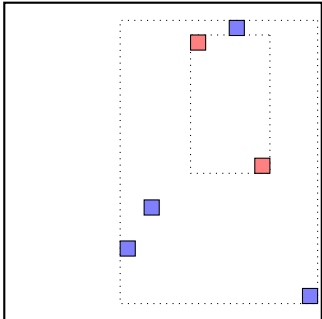
$S = 11.905245$

0 1 2 4 — 3 5



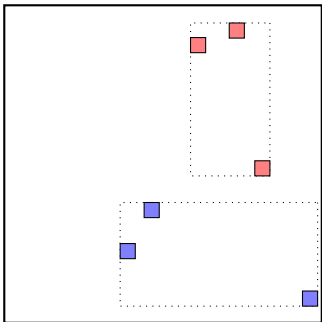
$S = 5.3026915$

0 1 3 4 — 2 5



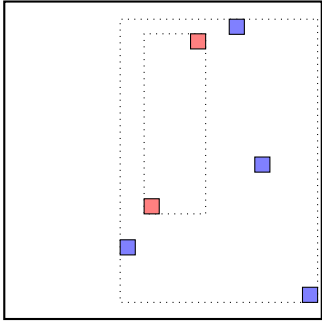
$S = 11.706051$

0 1 4 — 3 2 5



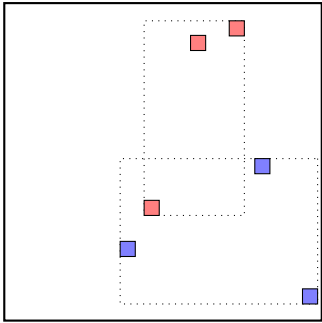
$S = 5.705201$

0 2 3 4 — 1 5



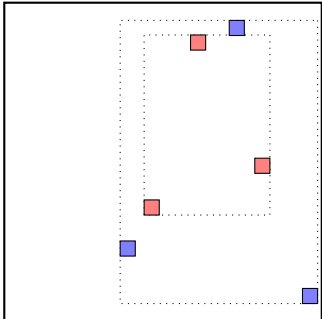
$$S = 11.723499$$

0 2 4 — 3 1 5



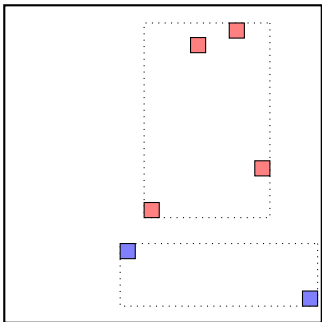
$$S = 8.4373255$$

0 3 4 — 2 1 5



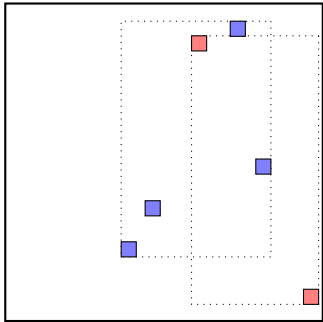
$$S = 13.748199$$

0 4 — 3 2 1 5



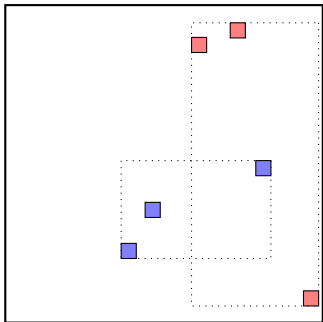
$$S = 6.447535$$

1 2 3 4 — 0 5



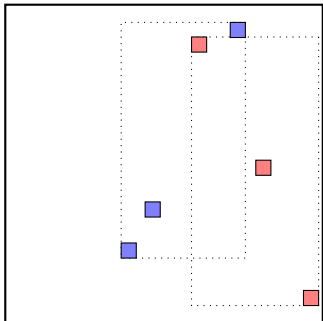
$$S = 12.14935$$

1 2 4 — 3 0 5



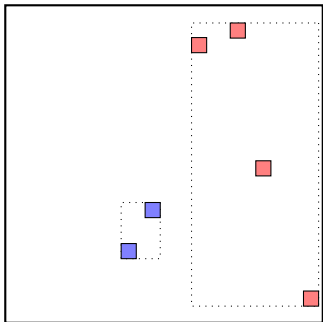
$$S = 8.862421$$

1 3 4 — 2 0 5



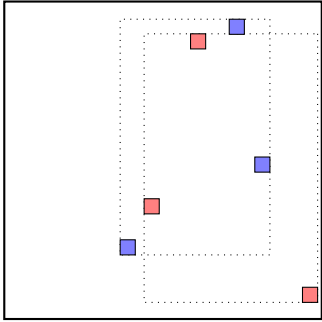
$$S = 11.095467$$

1 4 — 3 2 0 5



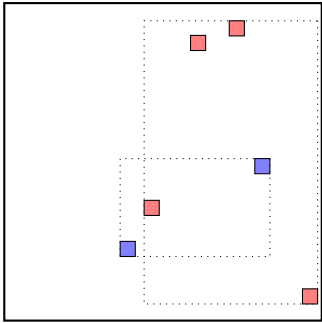
$$S = 6.681157$$

2 3 4 — 1 0 5



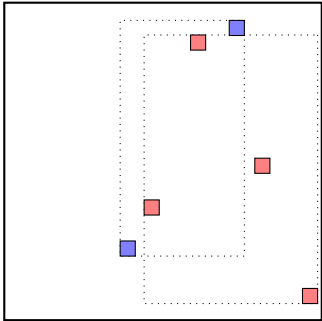
$S = 14.330893$

2 4 — 3 1 0 5



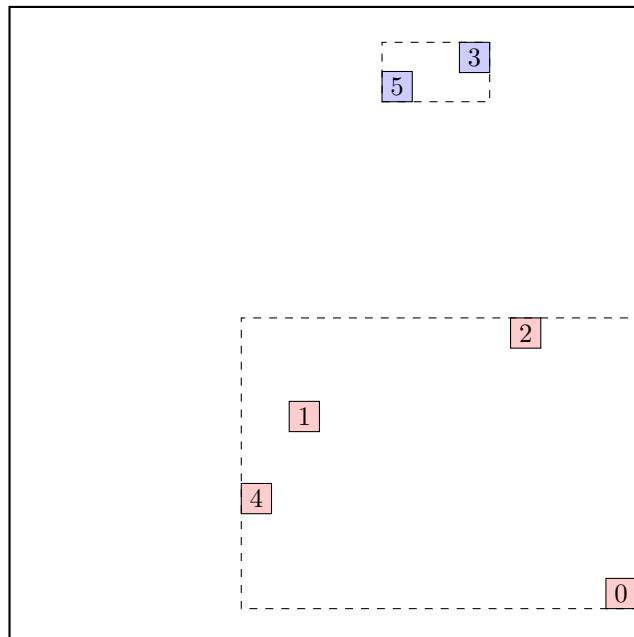
$S = 11.162466$

3 4 — 2 1 0 5



$S = 13.277009$

... the final split is:

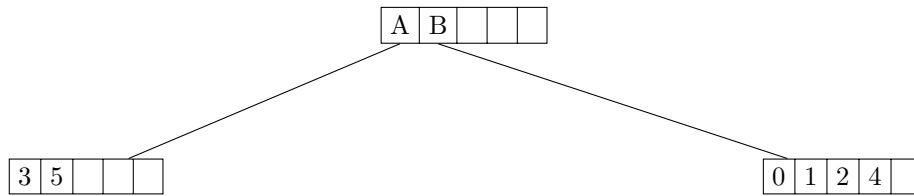


return from SPLIT-NODE

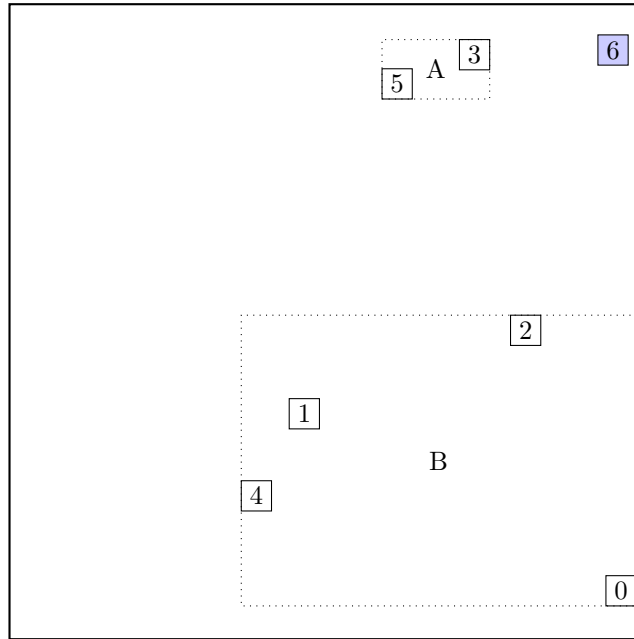
call ADJUST-TREE with R , node A and the new node
we are at the root
return from ADJUST-TREE

call INSERT *R*, #S(P :X 973/250 :Y 3797/1000)

structure view:

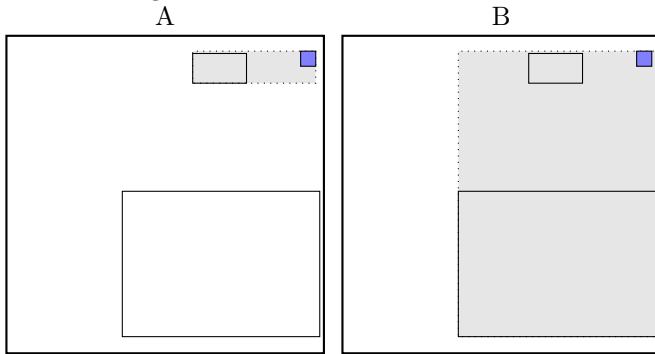


data view:



call CHOOSE-LEAF *R*, 6

choose among children:



old area: 0.27981588
 new area: 0.69027156
 extension: 0.41045567

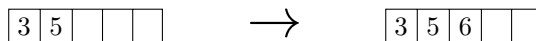
old area: 5.022876
 new area: 9.865524
 extension: 4.8426485

selected A

a leaf is found: A

return from CHOOSE-LEAF

the leaf A is not full, add the record.



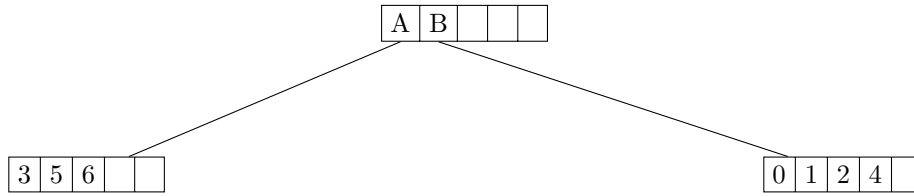
call ADJUST-TREE with *R*, node A
 update MBR of node A.

continue by adjusting the parent node root

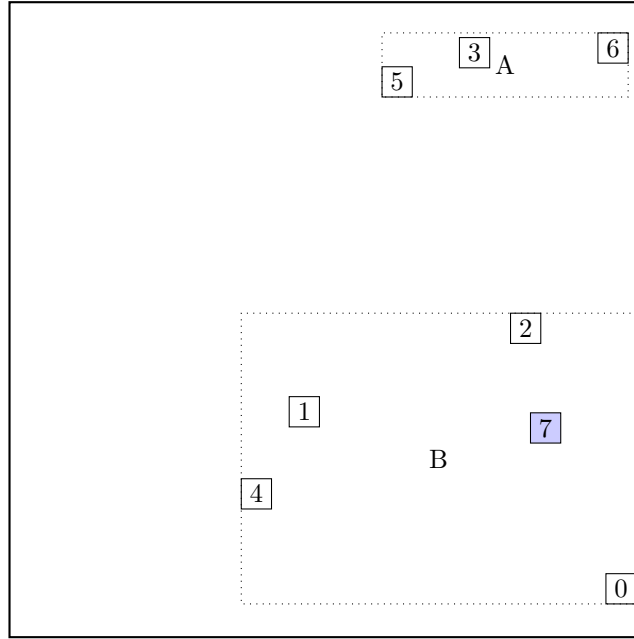
call ADJUST-TREE with R , node root
we are at the root
return from ADJUST-TREE

call INSERT R , #S(P :X 1723/500 :Y 321/250)

structure view:

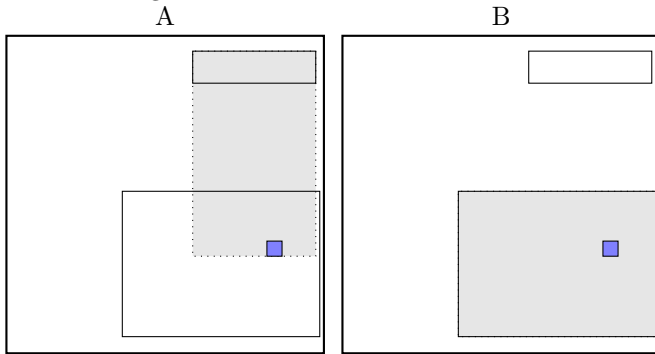


data view:



call CHOOSE-LEAF R , 7

choose among children:



old area: 0.69027156
 new area: 4.4167633
 extension: 3.7264917

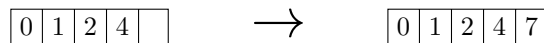
old area: 5.022876
 new area: 5.022876
 extension: 0.0

selected B

a leaf is found: B

return from CHOOSE-LEAF

the leaf B is not full, add the record.



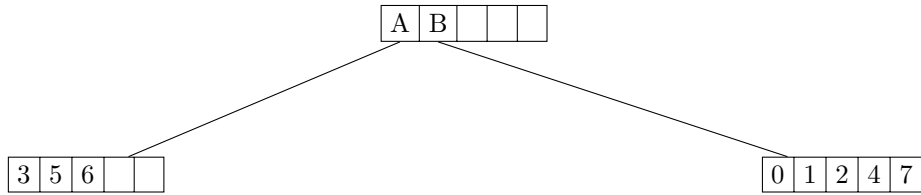
call ADJUST-TREE with R , node B
 update MBR of node B.

continue by adjusting the parent node root

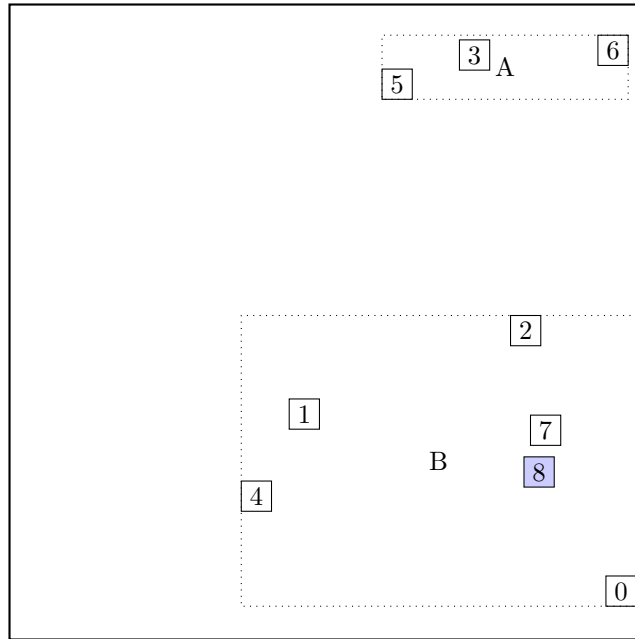
call ADJUST-TREE with R , node root
we are at the root
return from ADJUST-TREE

call INSERT *R*, #S(P :X 3403/1000 :Y 126/125)

structure view:

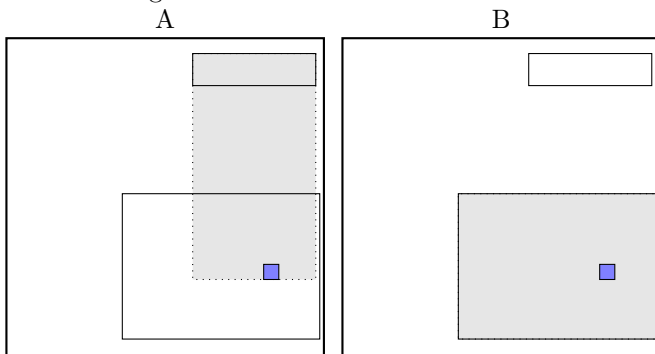


data view:



call CHOOSE-LEAF *R*, 8

choose among children:



old area: 0.69027156
new area: 4.8660913
extension: 4.17582

old area: 5.022876
new area: 5.022876
extension: 0.0

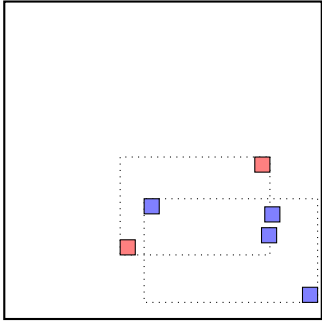
selected B

a leaf is found: B

return from CHOOSE-LEAF

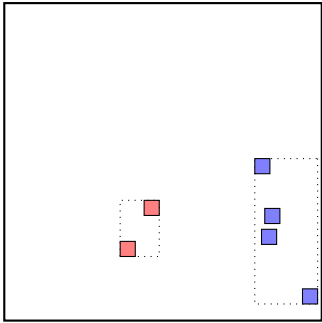
call SPLIT-NODE (bruteforce)

8 0 1 7 — 4 2



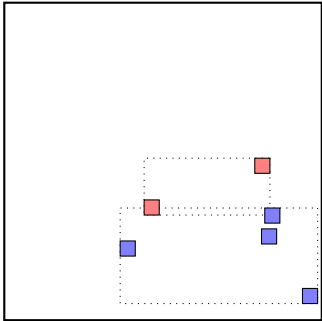
$$S = 5.71184$$

8 0 2 7 — 4 1



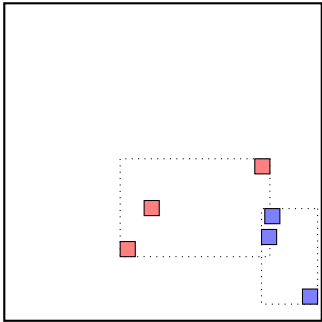
$$S = 1.9821442$$

8 0 4 7 — 2 1



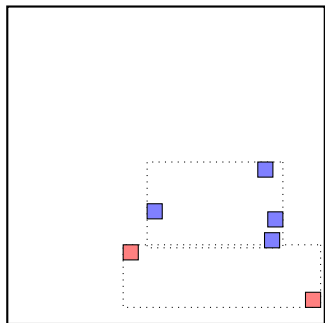
$$S = 4.5528956$$

8 0 7 — 4 2 1



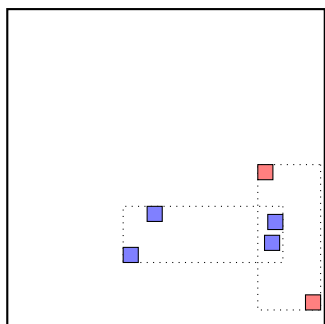
$$S = 3.5032828$$

8 1 2 7 — 4 0



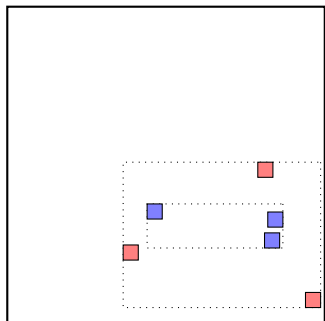
$S = 4.2011957$

8 1 4 7 — 2 0



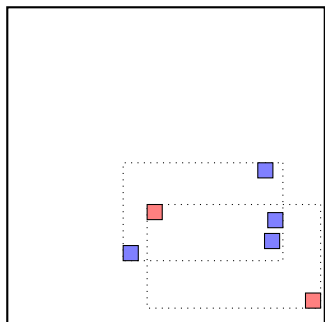
$S = 3.1679724$

8 1 7 — 4 2 0



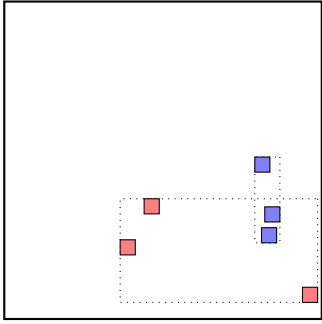
$S = 6.069944$

8 2 4 7 — 1 0



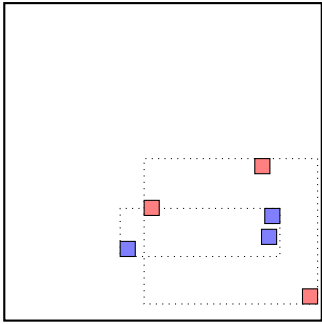
$S = 5.88278$

8 2 7 — 4 1 0



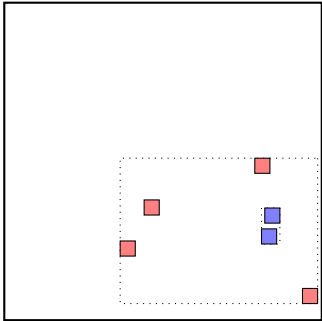
$S = 3.9578722$

8 4 7 — 2 1 0



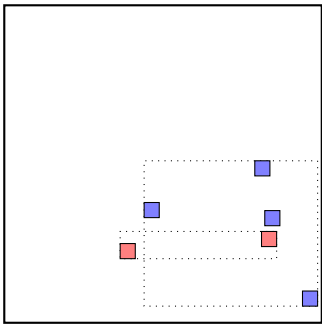
$S = 5.7571535$

8 7 — 4 2 1 0



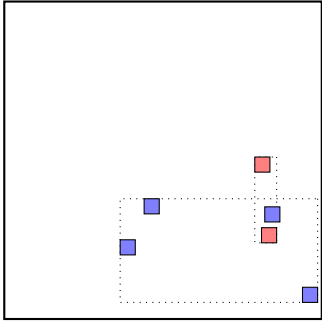
$S = 5.1385436$

0 1 2 7 — 4 8



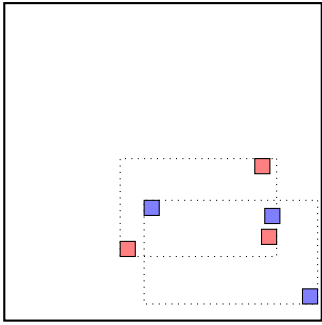
$S = 5.1584854$

0 1 4 7 — 2 8



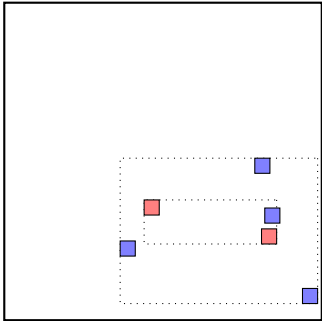
$$S = 3.9090672$$

0 1 7 — 4 2 8



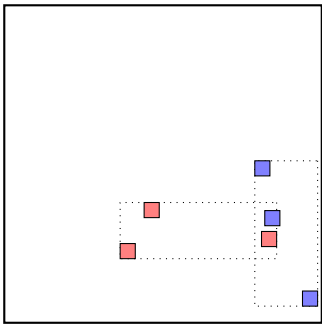
$$S = 5.827096$$

0 2 4 7 — 1 8



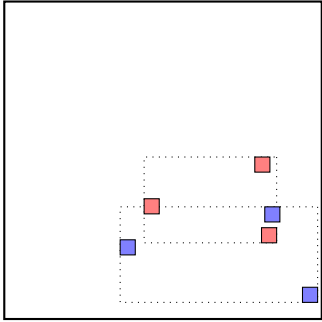
$$S = 6.044875$$

0 2 7 — 4 1 8



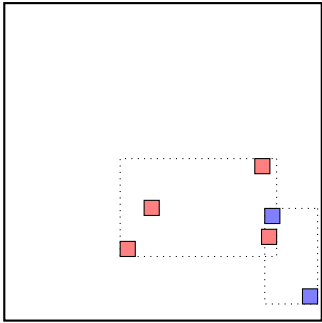
$$S = 3.1360236$$

0 4 7 — 2 1 8



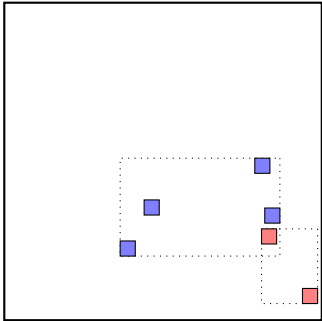
$S = 5.291223$

0 7 — 4 2 1 8



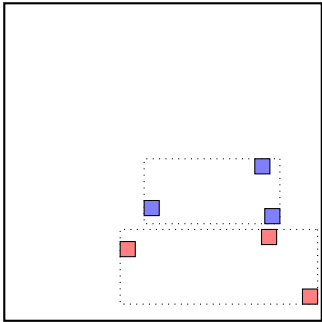
$S = 3.5641864$

1 2 4 7 — 0 8



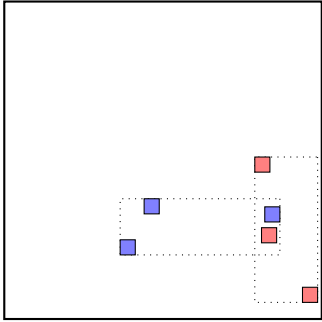
$S = 3.469431$

1 2 7 — 4 0 8



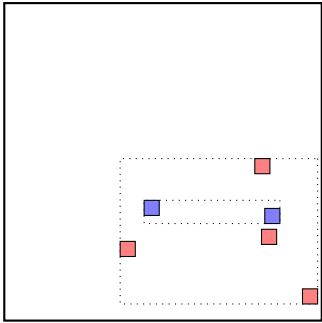
$S = 4.12342$

1 4 7 — 2 0 8



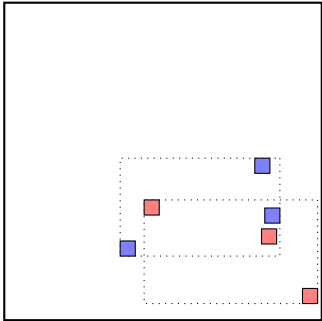
$$S = 3.1679724$$

1 7 — 4 2 0 8



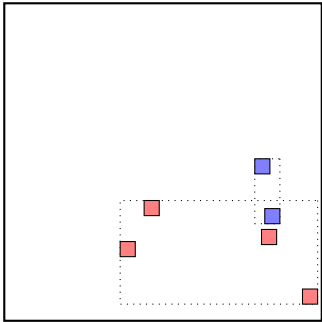
$$S = 5.574248$$

2 4 7 — 1 0 8



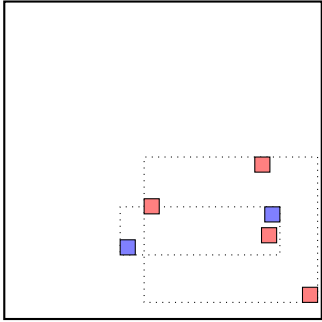
$$S = 5.88278$$

2 7 — 4 1 0 8



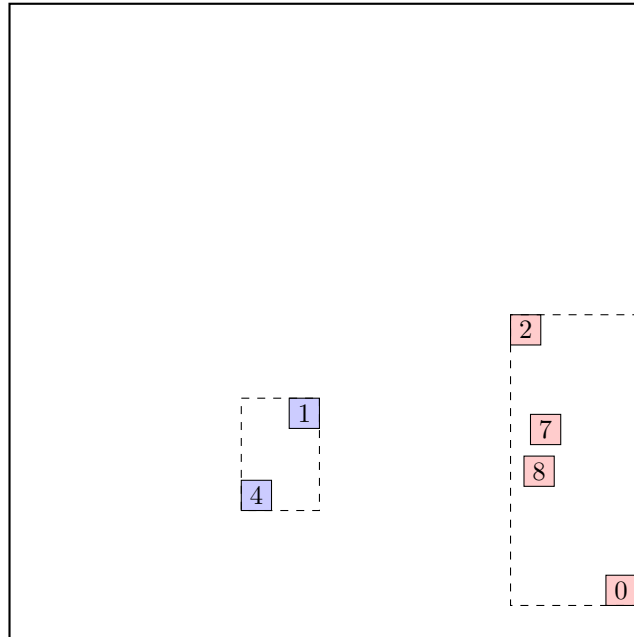
$$S = 3.86624$$

4 7 — 2 1 0 8



$S = 5.7571535$

... the final split is:



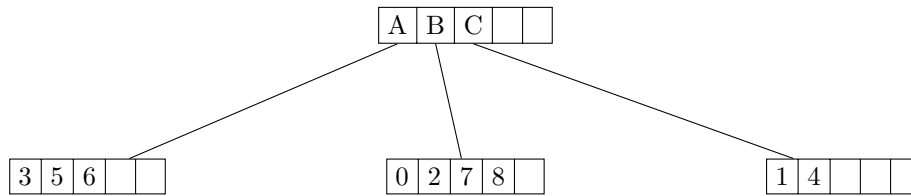
return from SPLIT-NODE

call ADJUST-TREE with R , node B and the new node
update MBR of node B.
add the new node to the parent node root

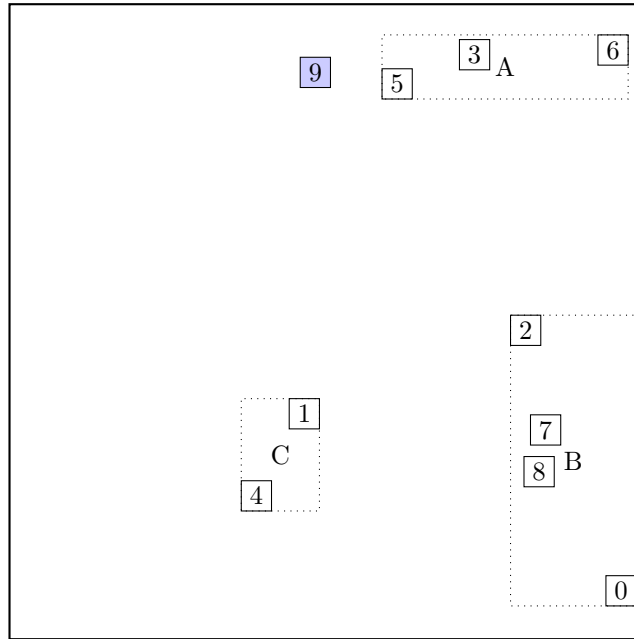
call ADJUST-TREE with R , node root
we are at the root
return from ADJUST-TREE

call INSERT R , #S(P :X 1923/1000 :Y 3649/1000)

structure view:

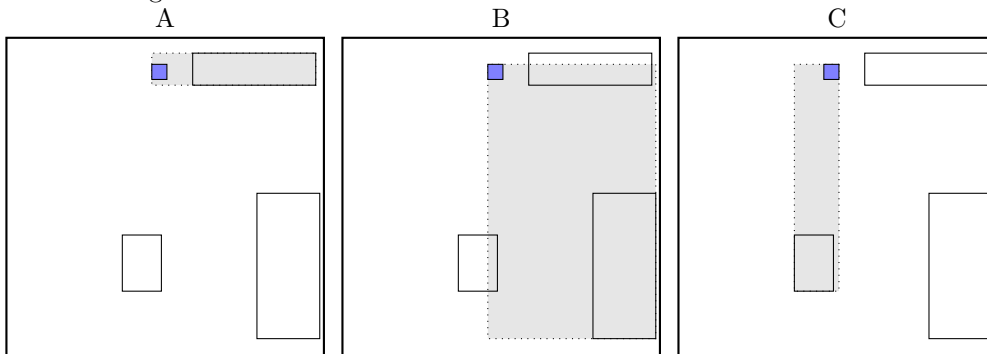


data view:



call CHOOSE-LEAF R , 9

choose among children:



old area: 0.69027156
 new area: 0.9196555
 extension: 0.22938395

old area: 1.5980132
 new area: 8.063639
 extension: 6.465626

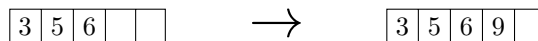
old area: 0.3841311
 new area: 1.7705901
 extension: 1.386459

selected A

a leaf is found: A

return from CHOOSE-LEAF

the leaf A is not full, add the record.



call ADJUST-TREE with R , node A

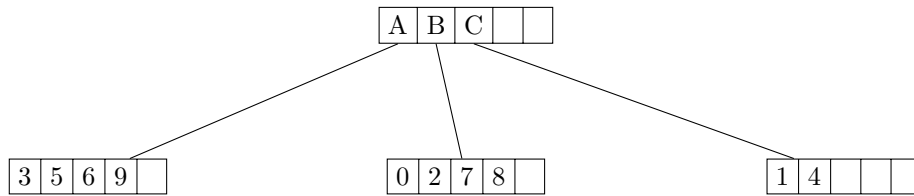
update MBR of node A.

continue by adjusting the parent node root

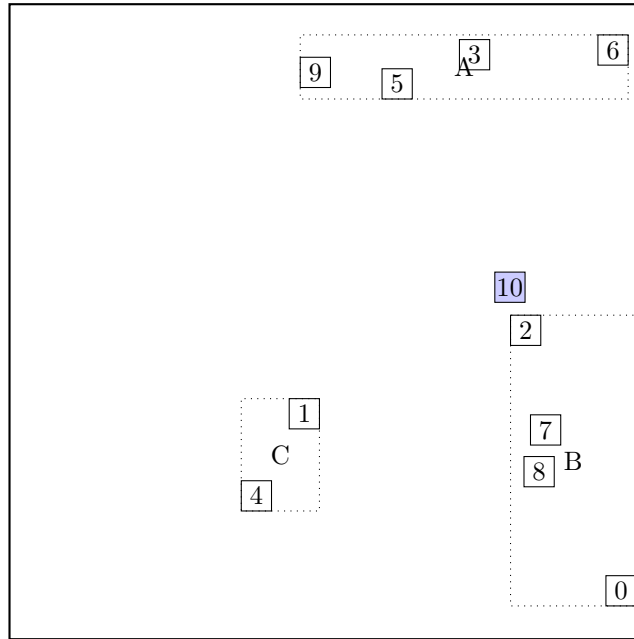
call ADJUST-TREE with R , node root
we are at the root
return from ADJUST-TREE

call INSERT R , #S(P :X 321/100 :Y 557/250)

structure view:

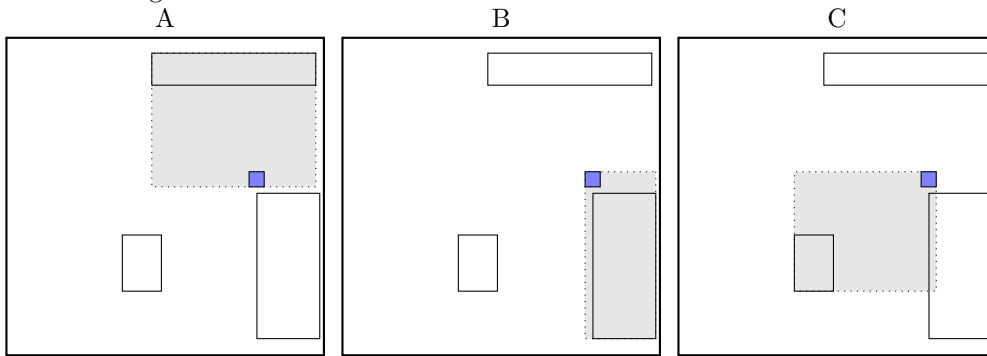


data view:



call CHOOSE-LEAF R , 10

choose among children:



old area: 0.9196555
 new area: 3.8369606
 extension: 2.917305

old area: 1.5980132
 new area: 2.0644799
 extension: 0.46646667

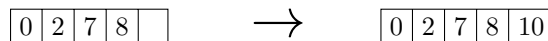
old area: 0.3841311
 new area: 2.9656599
 extension: 2.5815287

selected B

a leaf is found: B

return from CHOOSE-LEAF

the leaf B is not full, add the record.



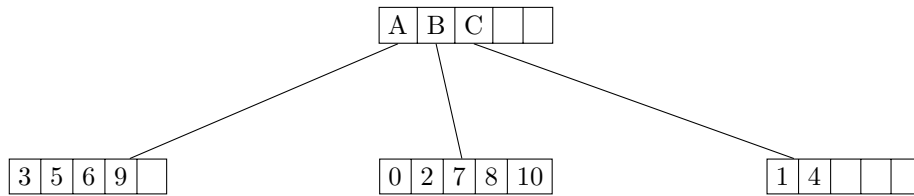
call ADJUST-TREE with R , node B
 update MBR of node B.

continue by adjusting the parent node root

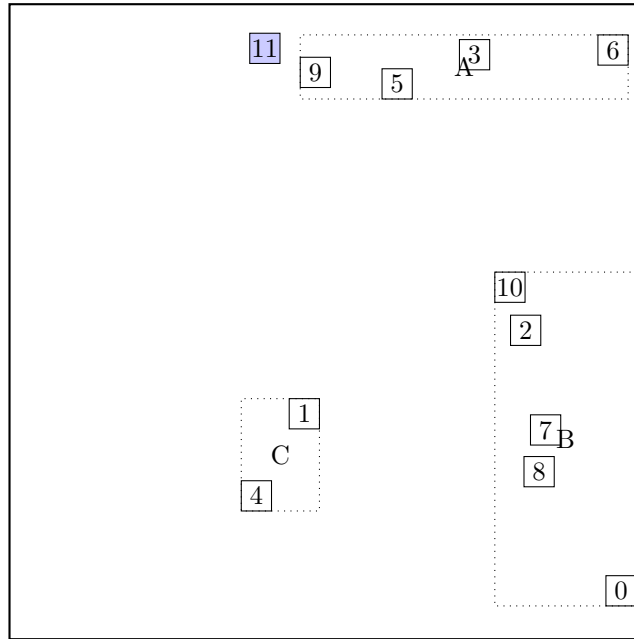
call ADJUST-TREE with R , node root
we are at the root
return from ADJUST-TREE

call INSERT R , #S(P :X 1589/1000 :Y 476/125)

structure view:

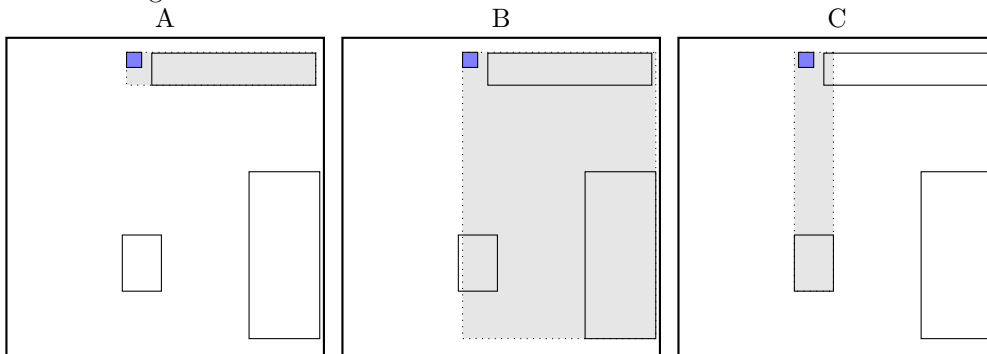


data view:



call CHOOSE-LEAF R , 11

choose among children:



old area: 0.9196555
new area: 1.0888047
extension: 0.16914922

old area: 2.0644799
new area: 9.682129
extension: 7.617649

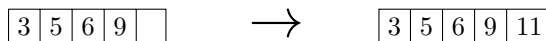
old area: 0.3841311
new area: 1.6337203
extension: 1.2495892

selected A

a leaf is found: A

return from CHOOSE-LEAF

the leaf A is not full, add the record.



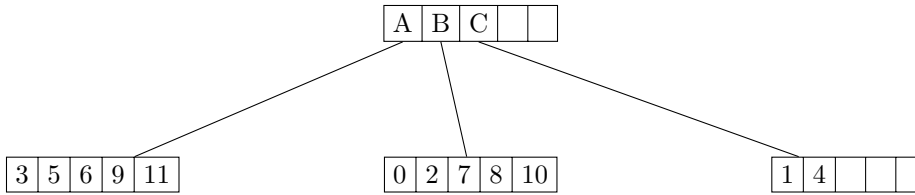
call ADJUST-TREE with R , node A
update MBR of node A.

continue by adjusting the parent node root

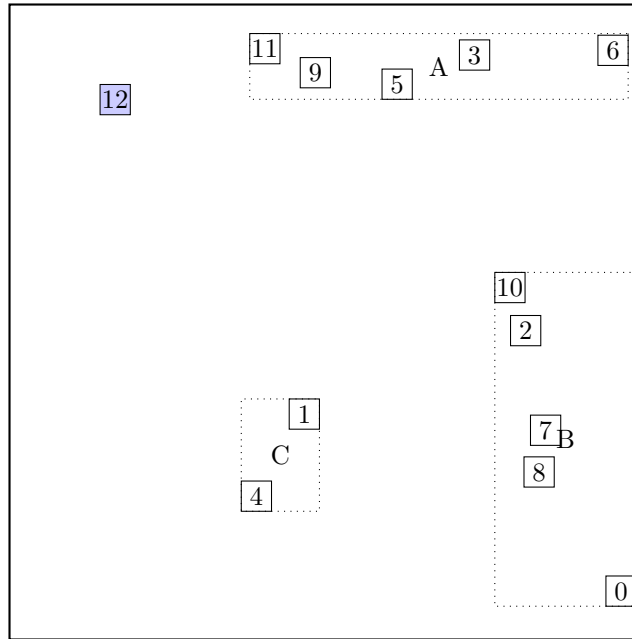
call ADJUST-TREE with R , node root
we are at the root
return from ADJUST-TREE

call INSERT *R*, #S(P :X 599/1000 :Y 3471/1000)

structure view:

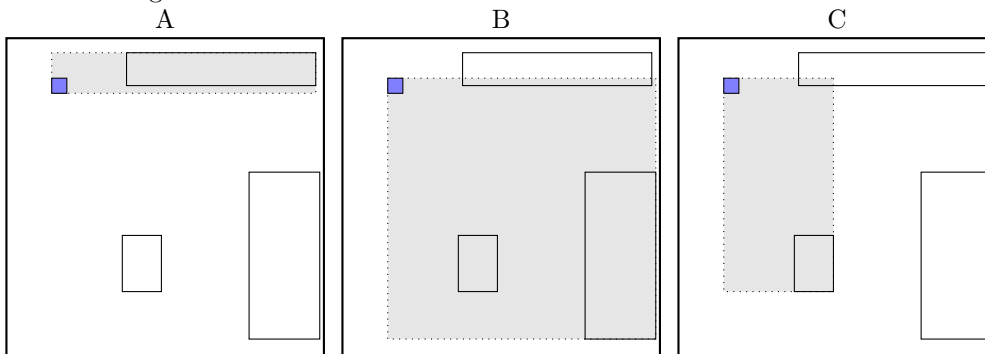


data view:



call CHOOSE-LEAF *R*, 12

choose among children:



old area: 1.0888047
 new area: 1.8757407
 extension: 0.7869359

old area: 2.0644799
 new area: 12.237246
 extension: 10.172766

old area: 0.3841311
 new area: 4.0961733
 extension: 3.712042

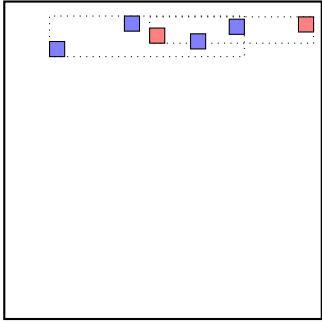
selected A

a leaf is found: A

return from CHOOSE-LEAF

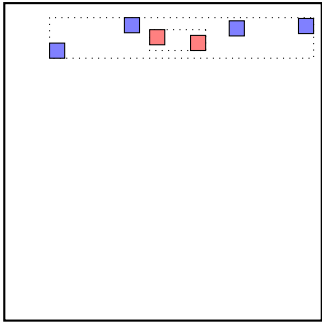
call SPLIT-NODE (bruteforce)

12 3 5 11 — 9 6



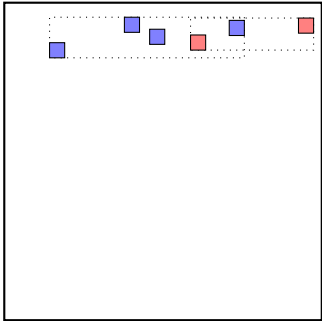
$$S = 2.1386605$$

12 3 6 11 — 9 5



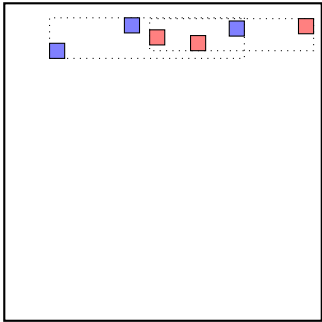
$$S = 2.0802565$$

12 3 9 11 — 6 5



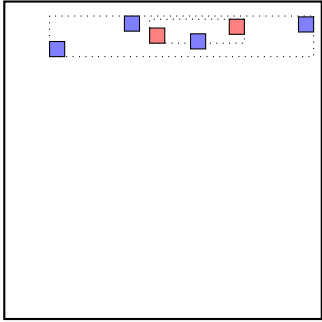
$$S = 2.0741203$$

12 3 11 — 9 6 5



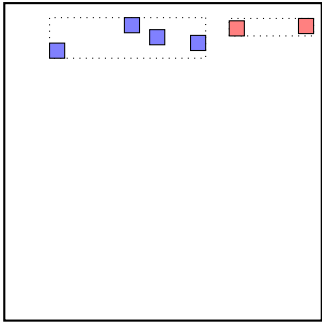
$$S = 2.3035043$$

12 5 6 11 — 9 3



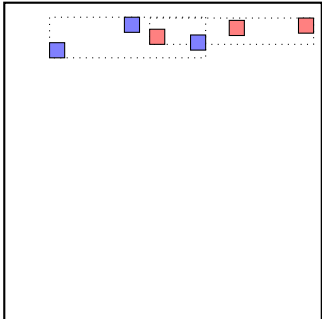
$$S = 2.2729416$$

12 5 9 11 — 6 3



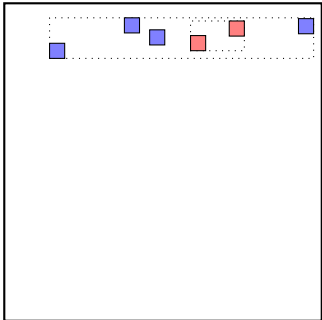
$$S = 1.3667004$$

12 5 11 — 9 6 3



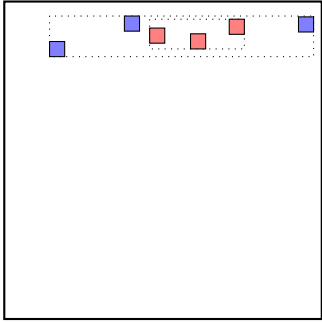
$$S = 1.8637164$$

12 6 9 11 — 5 3



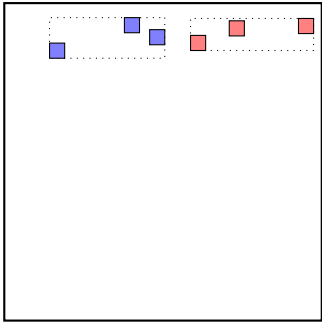
$$S = 2.1555565$$

12 6 11 — 9 5 3



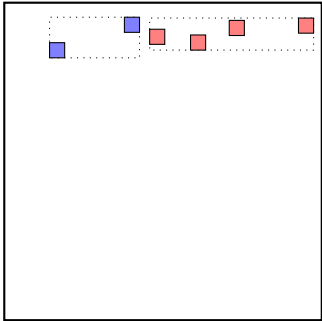
$$S = 2.3681696$$

12 9 11 — 6 5 3



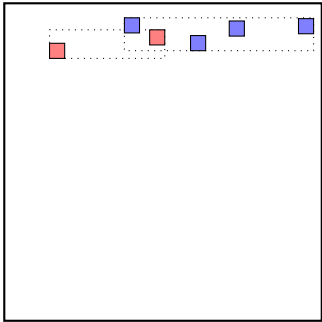
$$S = 1.5086595$$

12 11 — 9 6 5 3



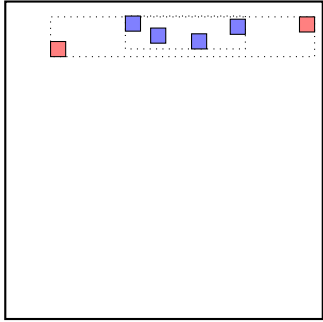
$$S = 1.5586856$$

3 5 6 11 — 9 12



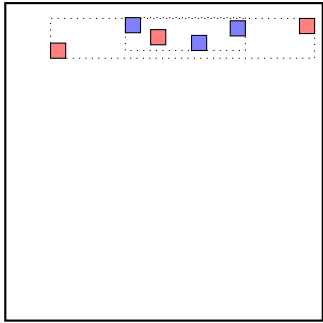
$$S = 1.6648765$$

3 5 9 11 — 6 12



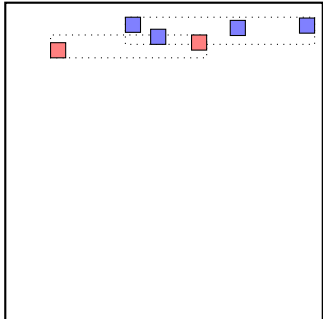
$S = 2.527662$

3 5 11 — 9 6 12



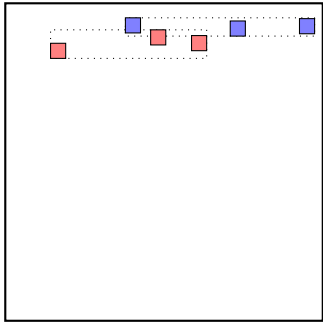
$S = 2.527662$

3 6 9 11 — 5 12



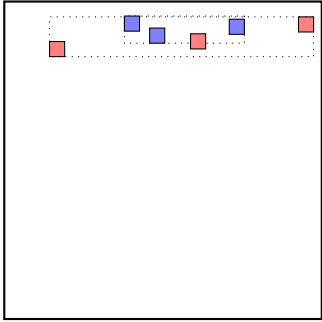
$S = 1.5222064$

3 6 11 — 9 5 12



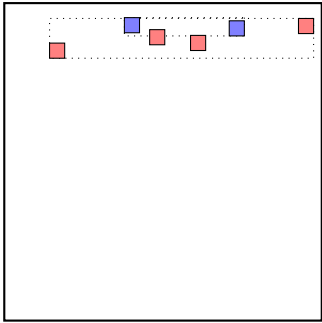
$S = 1.3862951$

3 9 11 — 6 5 12



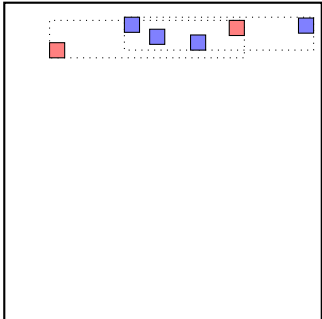
$$S = 2.4070502$$

3 11 — 9 6 5 12



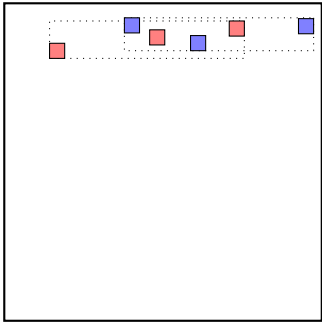
$$S = 2.221371$$

5 6 9 11 — 3 12



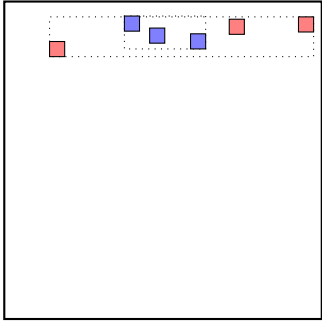
$$S = 2.3644195$$

5 6 11 — 9 3 12



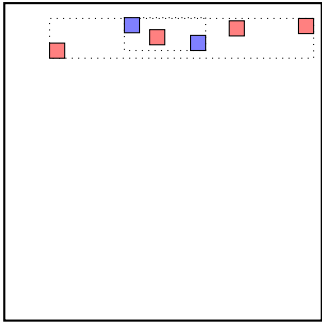
$$S = 2.3644195$$

5 9 11 — 6 3 12



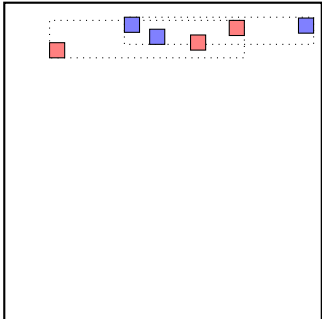
$$S = 2.3049422$$

5 11 — 9 6 3 12



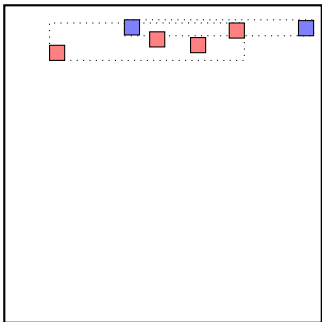
$$S = 2.3049422$$

6 9 11 — 5 3 12



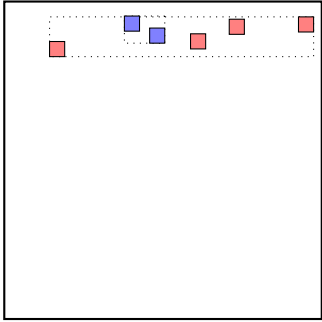
$$S = 2.1741915$$

6 11 — 9 5 3 12



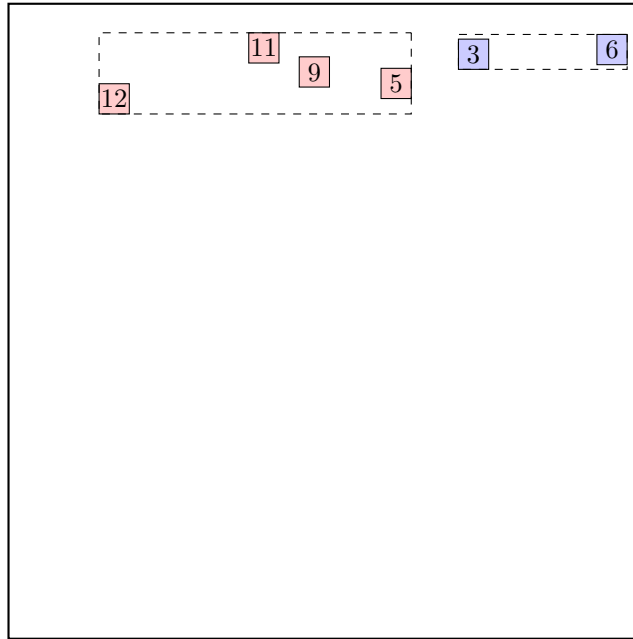
$$S = 1.8037474$$

9 11 — 6 5 3 12



$S = 2.0290232$

... the final split is:



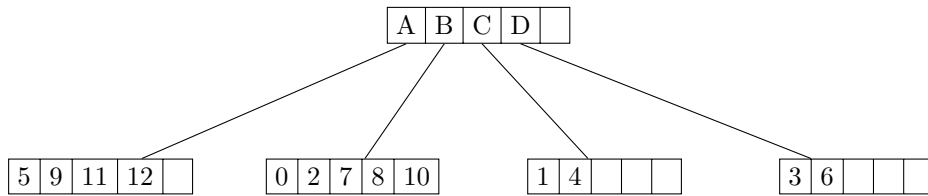
return from SPLIT-NODE

call ADJUST-TREE with R , node A and the new node
update MBR of node A.
add the new node to the parent node root

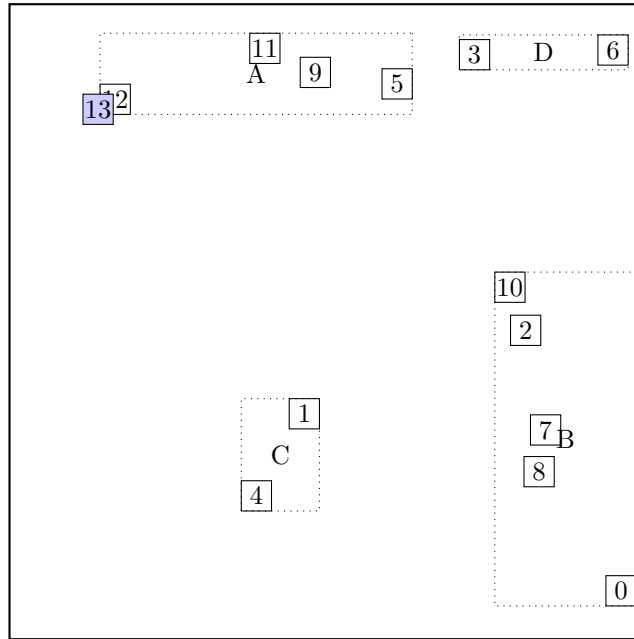
call ADJUST-TREE with R , node root
we are at the root
return from ADJUST-TREE

call INSERT *R*, #S(P :X 243/500 :Y 681/200)

structure view:

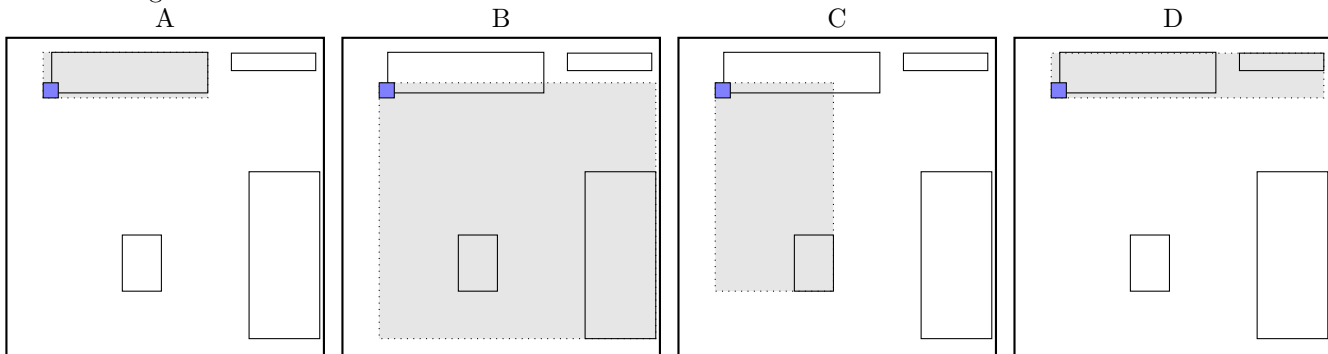


data view:



call CHOOSE-LEAF *R*, 13

choose among children:



old area: 1.1089048
new area: 1.3133339
extension: 0.20442903

old area: 2.0644799
new area: 12.3857155
extension: 10.321236

old area: 0.3841311
new area: 4.311948
extension: 3.9278167

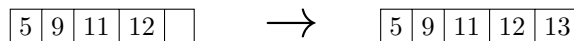
old area: 0.2577956
new area: 2.134751
extension: 1.8769555

selected A

a leaf is found: A

return from CHOOSE-LEAF

the leaf A is not full, add the record.



call ADJUST-TREE with *R*, node A

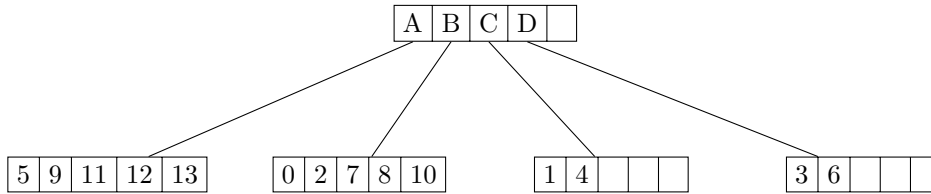
update MBR of node A.

continue by adjusting the parent node root

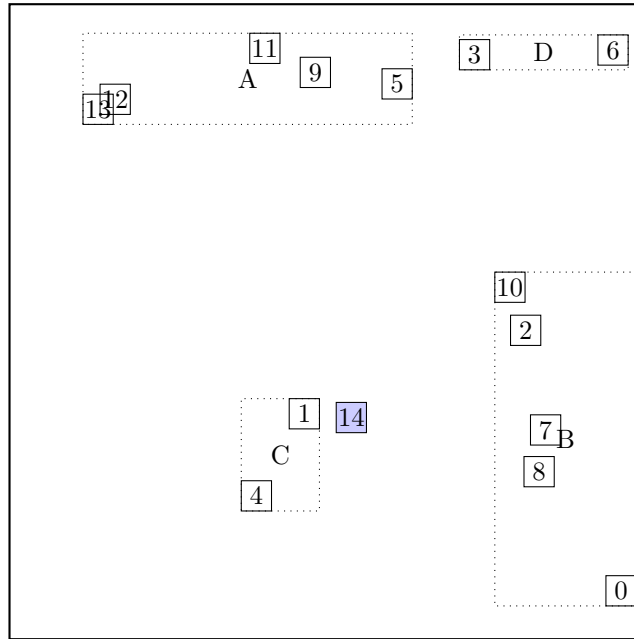
call ADJUST-TREE with R , node root
we are at the root
return from ADJUST-TREE

call INSERT *R*, #S(P :X 2161/1000 :Y 683/500)

structure view:

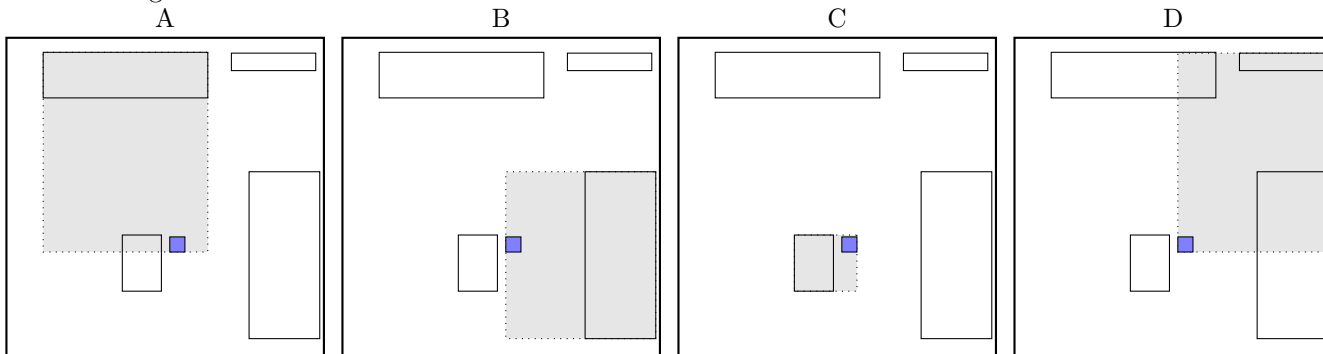


data view:



call CHOOSE-LEAF *R*, 14

choose among children:



old area: 1.3133339
 new area: 5.754276
 extension: 4.440942

old area: 2.0644799
 new area: 4.380672
 extension: 2.3161922

old area: 0.3841311
 new area: 0.61520404
 extension: 0.23107293

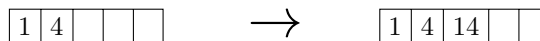
old area: 0.2577956
 new area: 5.08046
 extension: 4.8226643

selected C

a leaf is found: C

return from CHOOSE-LEAF

the leaf C is not full, add the record.



call ADJUST-TREE with *R*, node C

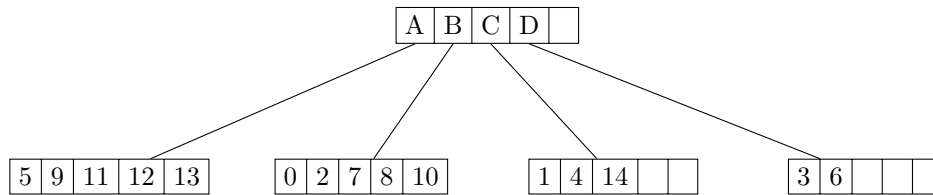
update MBR of node C.

continue by adjusting the parent node root

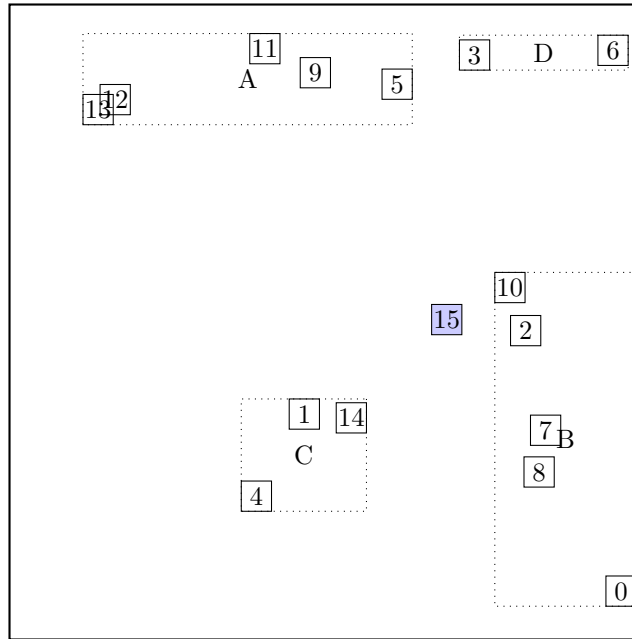
call ADJUST-TREE with R , node root
we are at the root
return from ADJUST-TREE

call INSERT *R*, #S(P :X 349/125 :Y 252/125)

structure view:

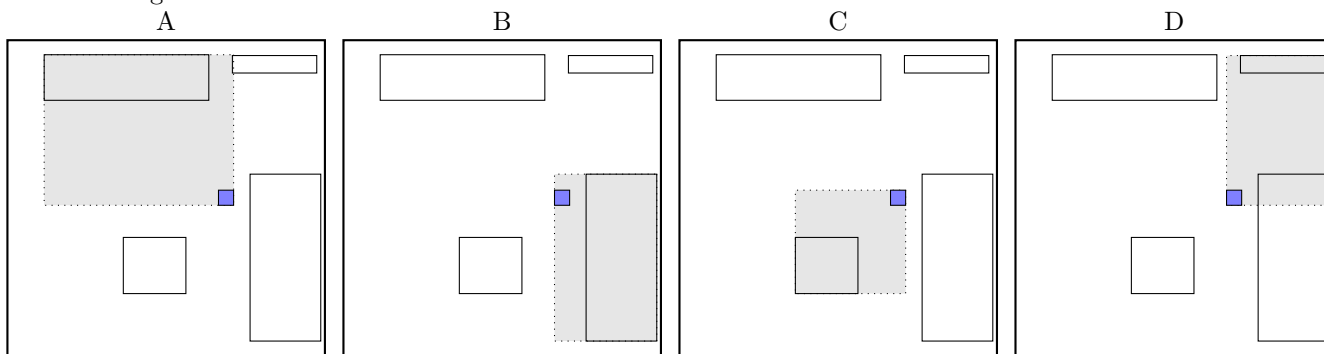


data view:



call CHOOSE-LEAF *R*, 15

choose among children:



old area: 1.3133339
new area: 4.991952
extension: 3.678618

old area: 2.0644799
new area: 2.9874237
extension: 0.92294384

old area: 0.61520404
new area: 1.9959121
extension: 1.380708

old area: 0.2577956
new area: 2.5752993
extension: 2.3175037

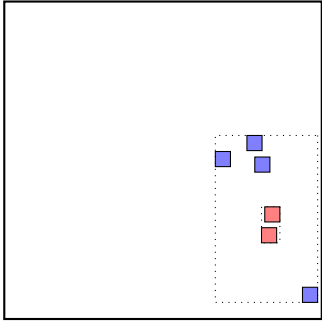
selected B

a leaf is found: B

return from CHOOSE-LEAF

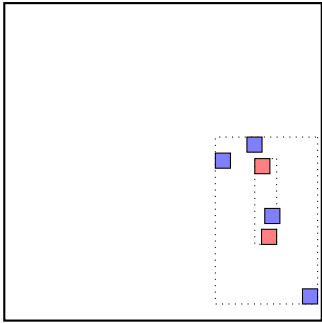
call SPLIT-NODE (bruteforce)

15 0 2 10 — 8 7



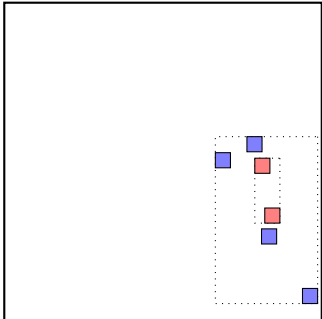
$$S = 3.1030915$$

15 0 7 10 — 8 2



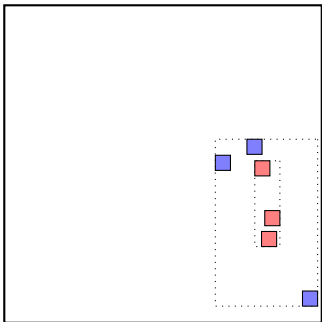
$$S = 3.3154388$$

15 0 8 10 — 7 2



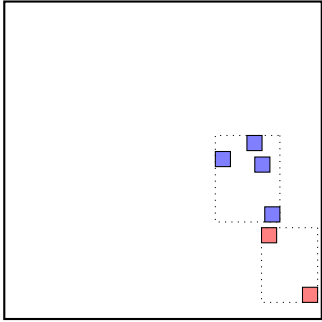
$$S = 3.2726116$$

15 0 10 — 8 7 2



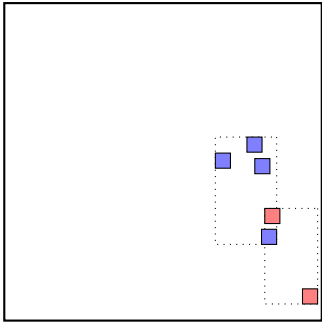
$$S = 3.3642438$$

15 2 7 10 — 8 0



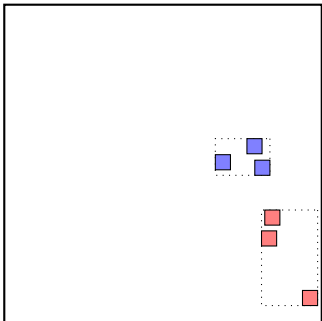
$S = 1.7100716$

15 2 8 10 — 7 0



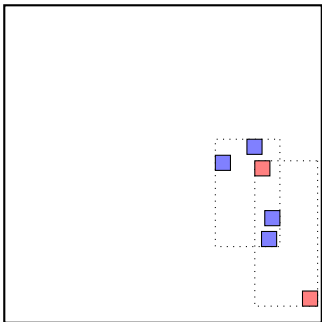
$S = 2.0351556$

15 2 10 — 8 7 0



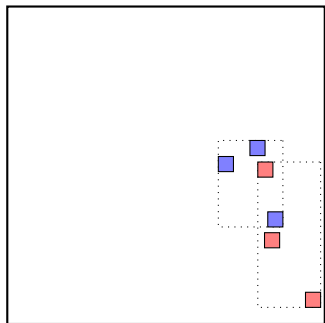
$S = 1.2880576$

15 7 8 10 — 2 0



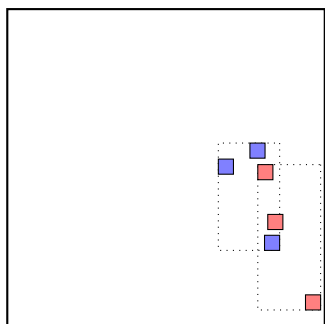
$S = 2.8106928$

15 7 10 — 8 2 0



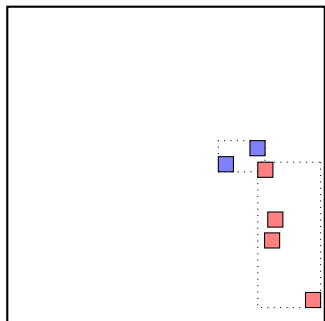
$S = 2.5749889$

15 8 10 — 7 2 0



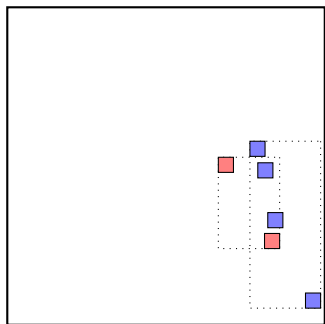
$S = 2.7496329$

15 10 — 8 7 2 0



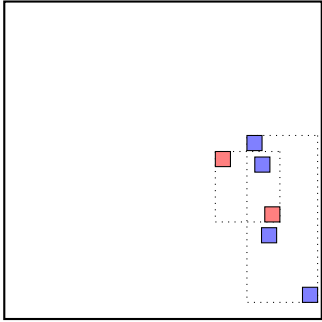
$S = 1.852629$

0 2 7 10 — 8 15



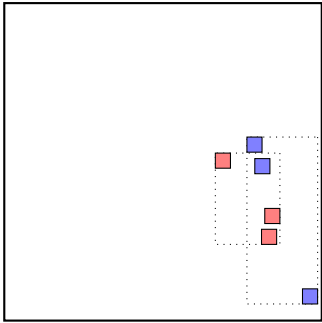
$S = 3.0441675$

0 2 8 10 — 7 15



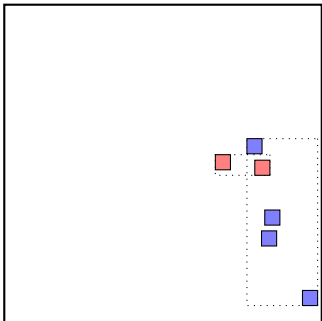
$$S = 2.8604076$$

0 2 10 — 8 7 15



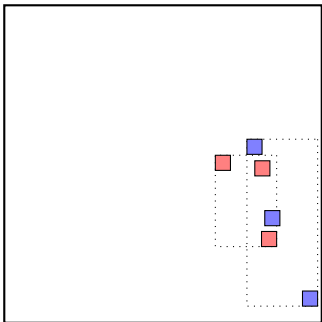
$$S = 3.0961118$$

0 7 8 10 — 2 15



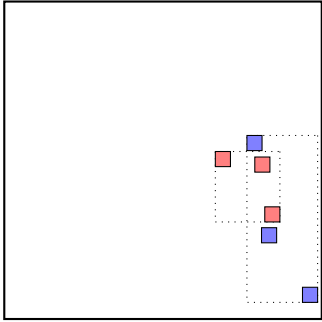
$$S = 2.2615857$$

0 7 10 — 8 2 15



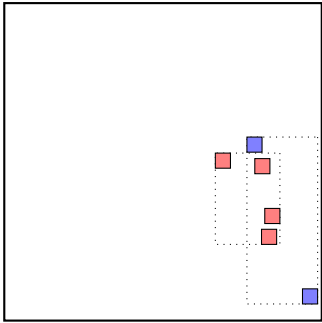
$$S = 3.0441675$$

0 8 10 — 7 2 15



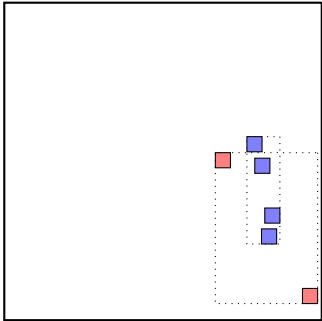
$S = 2.8604076$

0 10 — 8 7 2 15



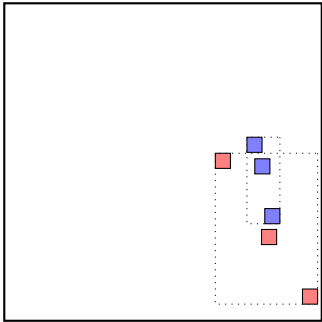
$S = 3.0961118$

2 7 8 10 — 0 15



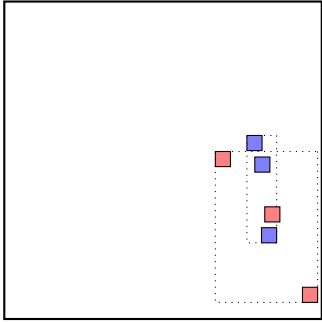
$S = 3.3197074$

2 7 10 — 8 0 15



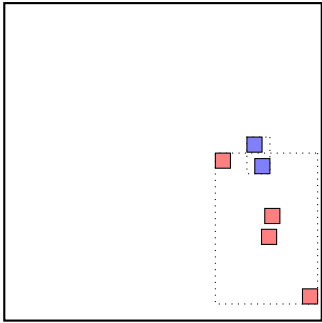
$S = 3.1993716$

2 8 10 — 7 0 15



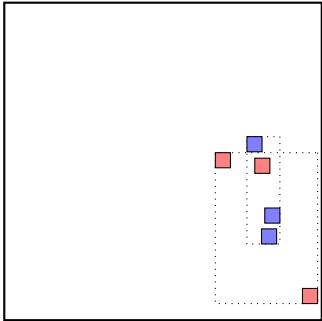
$S = 3.2586475$

2 10 — 8 7 0 15



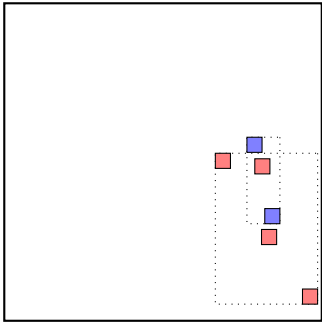
$S = 2.8480275$

7 8 10 — 2 0 15



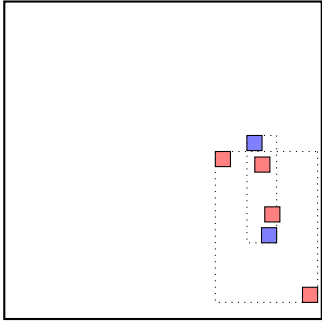
$S = 3.3197074$

7 10 — 8 2 0 15



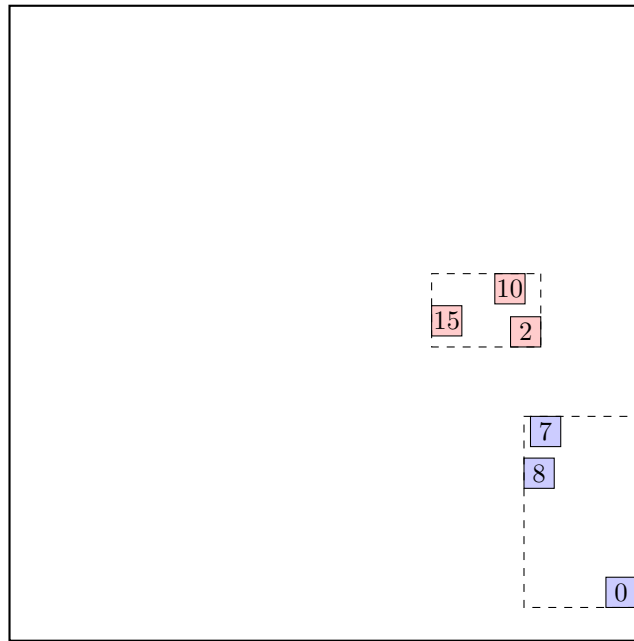
$S = 3.1993716$

8 10 — 7 2 0 15



$$S = 3.2586475$$

... the final split is:



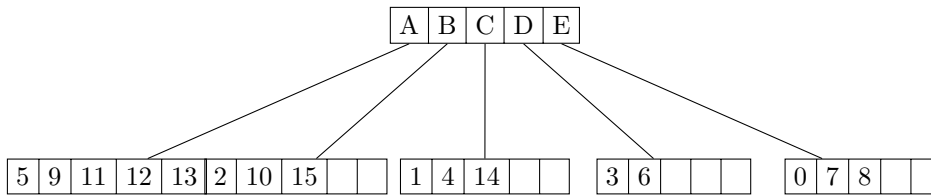
return from SPLIT-NODE

call ADJUST-TREE with R , node B and the new node
update MBR of node B.
add the new node to the parent node root

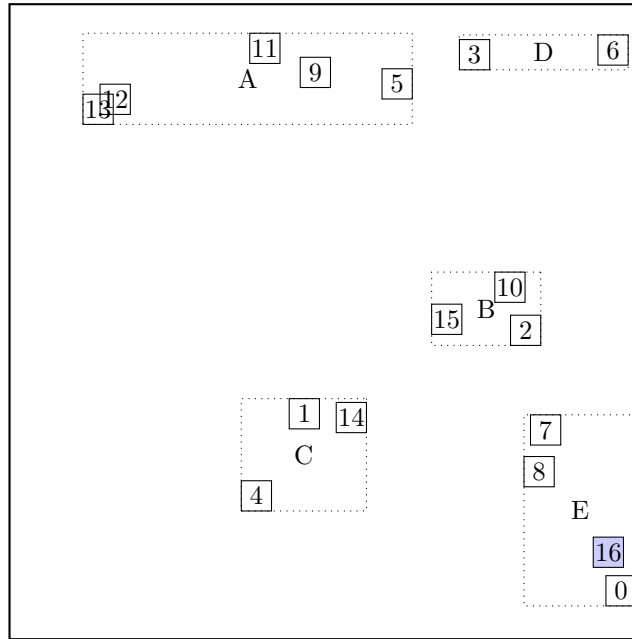
call ADJUST-TREE with R , node root
we are at the root
return from ADJUST-TREE

call INSERT R , #S(P :X 3861/1000 :Y 19/40)

structure view:

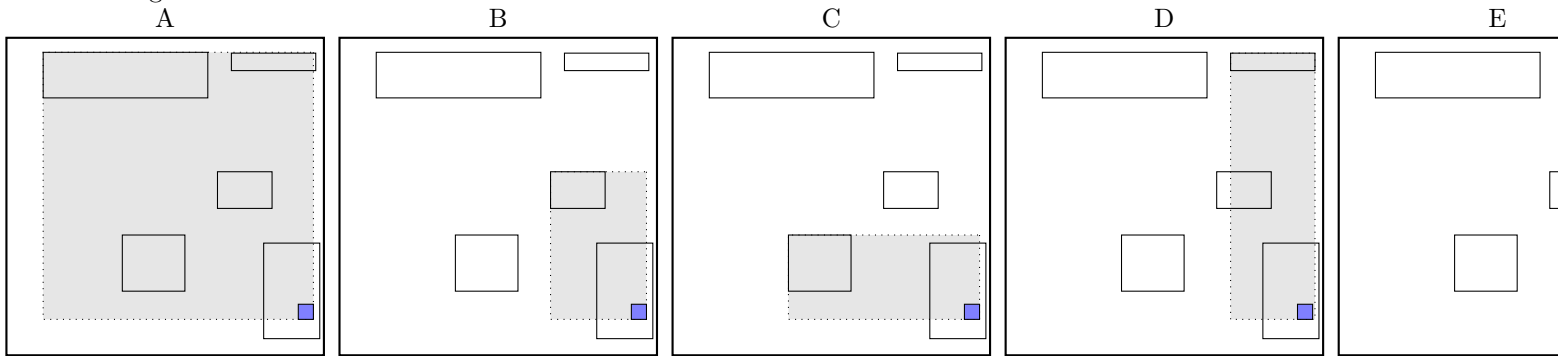


data view:



call CHOOSE-LEAF R , 16

choose among children:



old area: 1.3133339
new area: 12.630475
extension: 11.317142

old area: 0.35016975
new area: 2.4783564
extension: 2.1281867

old area: 0.61520404
new area: 2.821248
extension: 2.206044

old area: 0.2577956
new area: 3.9305508
extension: 3.6727553

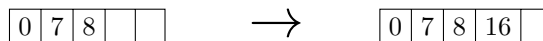
old area: 0.9378
new area: 0.9378
extension: 0

selected E

a leaf is found: E

return from CHOOSE-LEAF

the leaf E is not full, add the record.



call ADJUST-TREE with R , node E

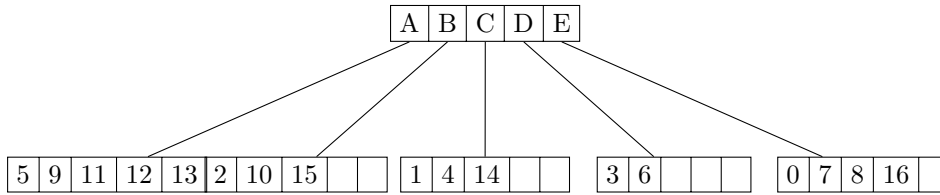
update MBR of node E.

continue by adjusting the parent node root

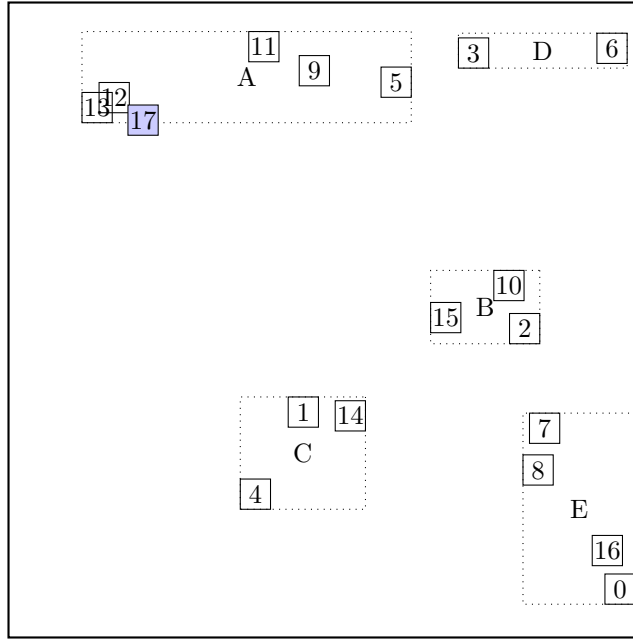
call ADJUST-TREE with R , node root
we are at the root
return from ADJUST-TREE

call INSERT *R*, #S(P :X 79/100 :Y 1661/500)

structure view:

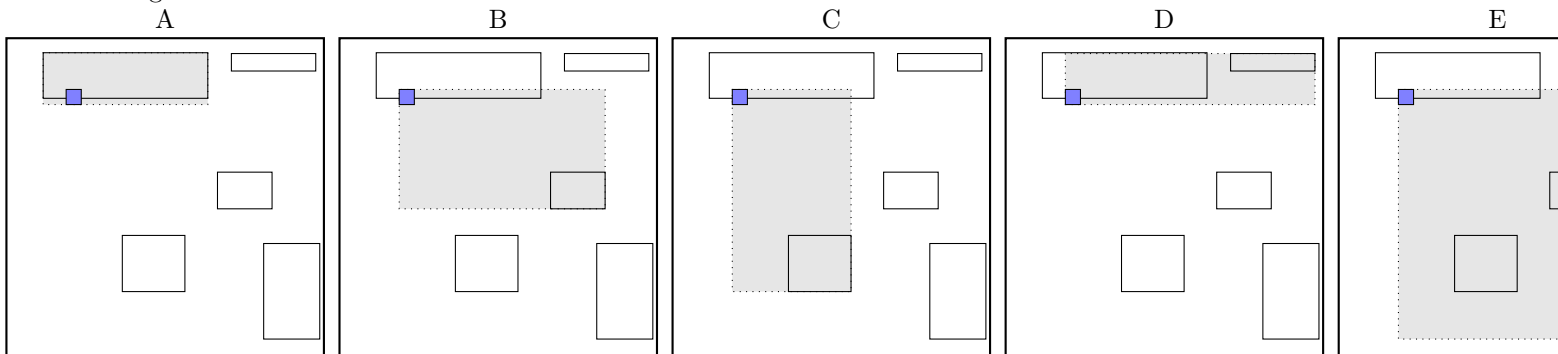


data view:



call CHOOSE-LEAF *R*, 17

choose among children:



old area: 1.3133339
new area: 1.4941077
extension: 0.18077386

old area: 0.35016975
new area: 4.3011956
extension: 3.951026

old area: 0.61520404
new area: 4.200854
extension: 3.5856498

old area: 0.2577956
new area: 2.228849
extension: 1.9710534

old area: 0.9378
new area: 11.0
extension: 10.14

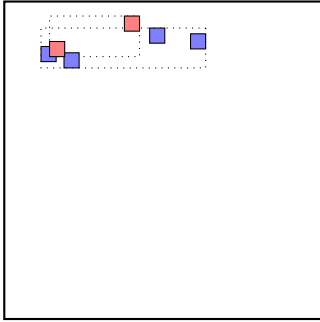
selected A

a leaf is found: A

return from CHOOSE-LEAF

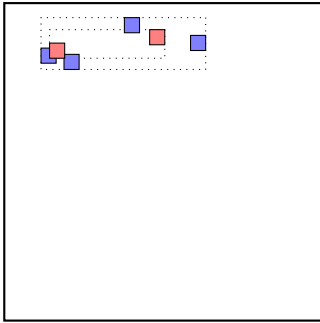
call SPLIT-NODE (bruteforce)

17 5 9 13 — 12 11



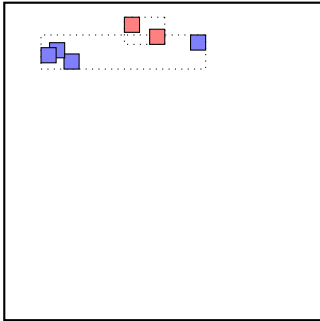
$$S = 1.7868353$$

17 5 11 13 — 12 9



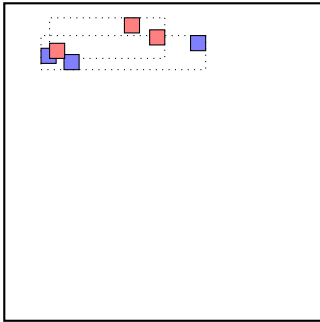
$$S = 2.0701795$$

17 5 12 13 — 11 9



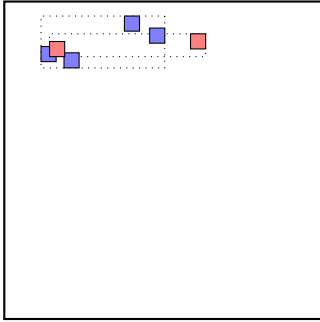
$$S = 1.1739833$$

17 5 13 — 12 11 9



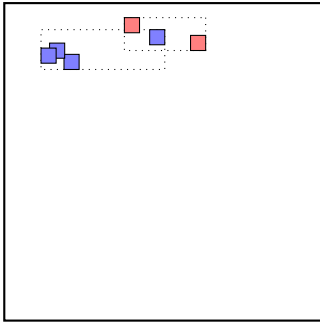
$$S = 1.8006654$$

17 9 11 13 — 12 5



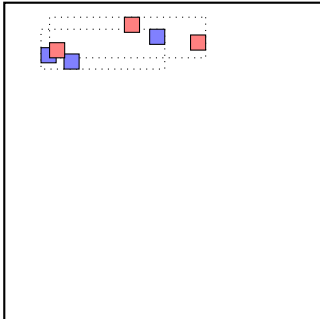
$$S = 1.7466114$$

17 9 12 13 — 11 5



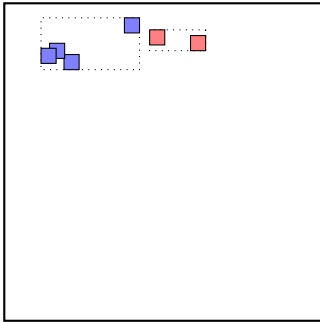
$$S = 1.3303235$$

17 9 13 — 12 11 5



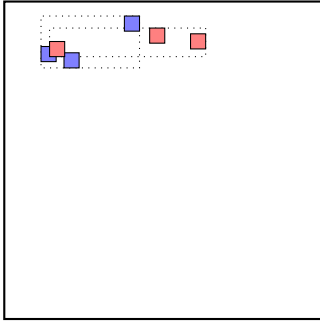
$$S = 1.9716034$$

17 11 12 13 — 9 5



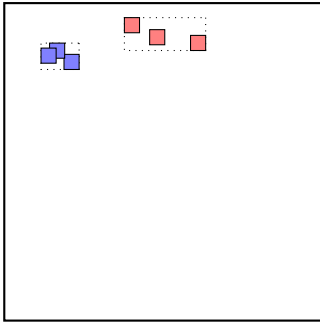
$$S = 1.0983737$$

17 11 13 — 12 9 5



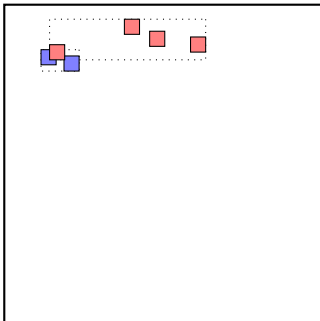
$$S = 1.6744273$$

17 12 13 — 11 9 5



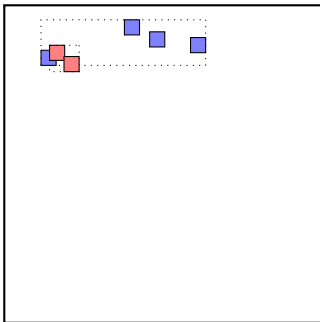
$$S = 0.6435208$$

17 13 — 12 11 9 5



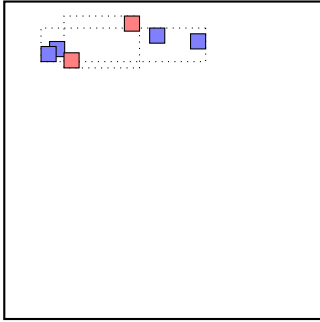
$$S = 1.2515367$$

5 9 11 13 — 12 17



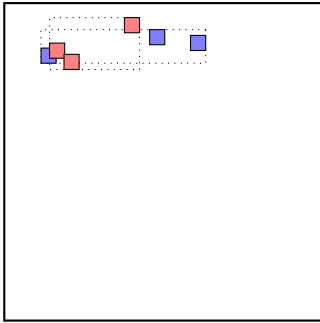
$$S = 1.4497928$$

5 9 12 13 — 11 17



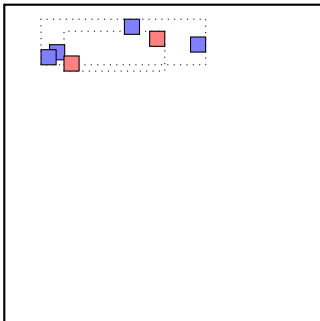
$$S = 1.6523454$$

5 9 13 — 12 11 17



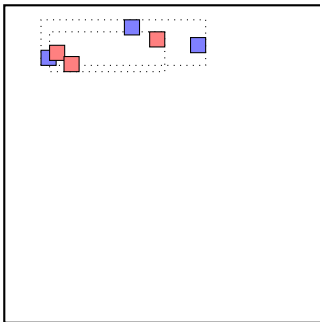
$$S = 1.7833715$$

5 11 12 13 — 9 17



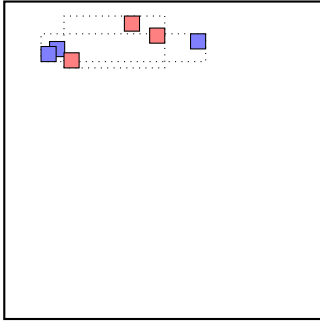
$$S = 2.0158243$$

5 11 13 — 12 9 17



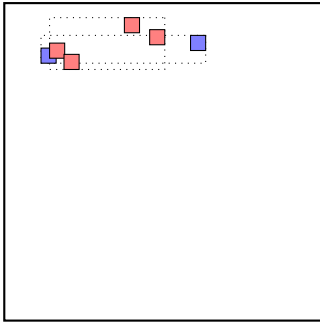
$$S = 2.1164816$$

5 12 13 — 11 9 17



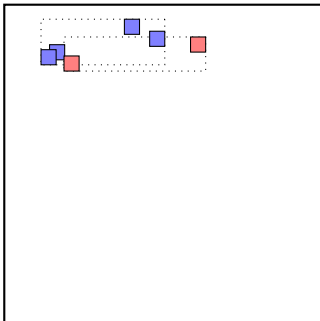
$$S = 1.7159413$$

5 13 — 12 11 9 17



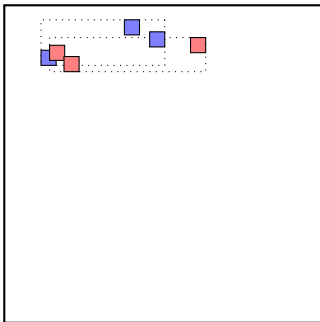
$$S = 1.8469673$$

9 11 12 13 — 5 17



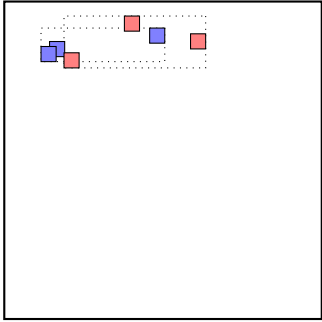
$$S = 1.8322842$$

9 11 13 — 12 5 17



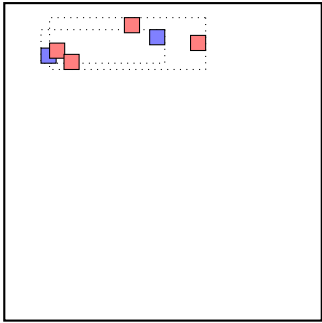
$$S = 1.9184252$$

9 12 13 — 11 5 17



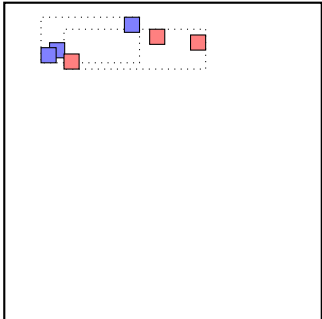
$$S = 2.012391$$

9 13 — 12 11 5 17



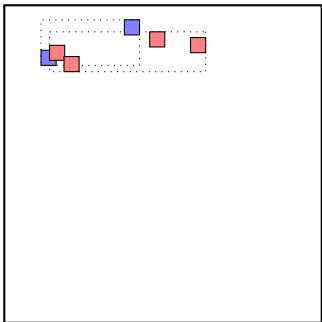
$$S = 2.1434174$$

11 12 13 — 9 5 17



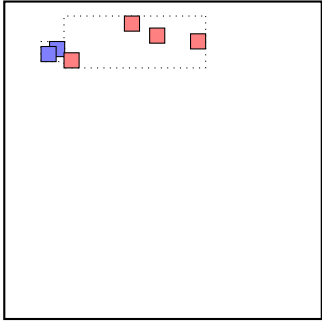
$$S = 1.7733063$$

11 13 — 12 9 5 17



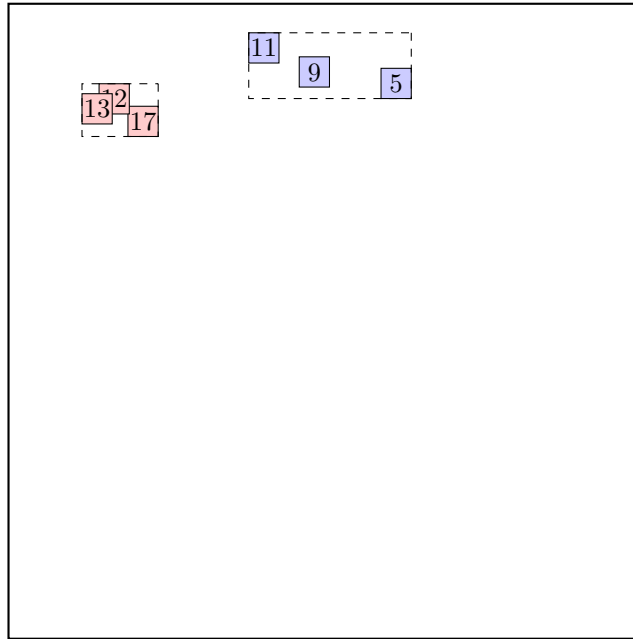
$$S = 1.8739632$$

12 13 — 11 9 5 17



$S = 1.3688215$

... the final split is:



return from SPLIT-NODE

call ADJUST-TREE with R , node A and the new node

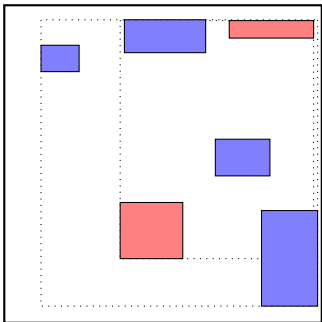
update MBR of node A.

add the new node to the parent node root

Parent node root is full, promote split (create a new parent)

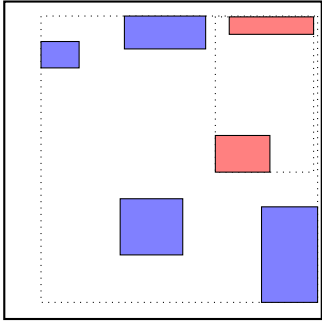
call SPLIT-NODE (bruteforce)

F A B E — D C



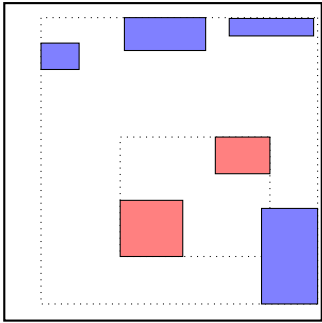
$S = 21.918583$

F A C E — D B



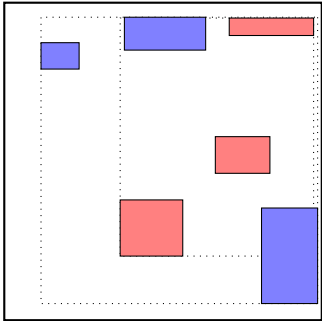
$$S = 16.530493$$

F A D E — C B



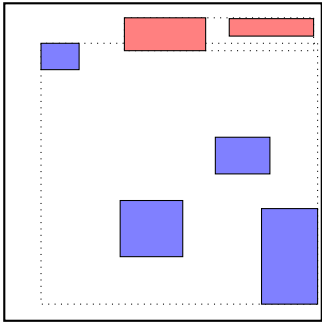
$$S = 16.990273$$

F A E — D C B



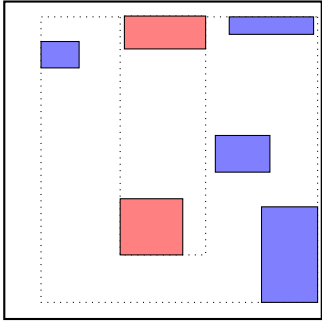
$$S = 21.918583$$

F B C E — D A



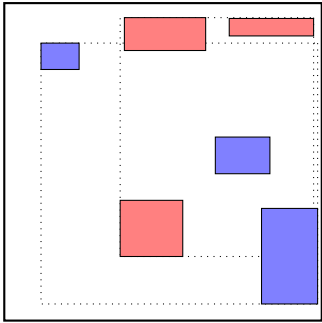
$$S = 13.716015$$

F B D E — C A



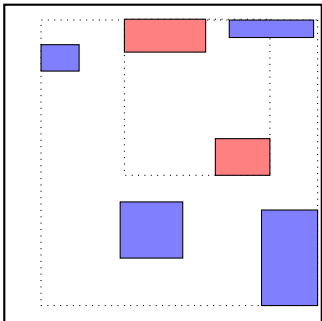
$$S = 17.394003$$

F B E — D C A



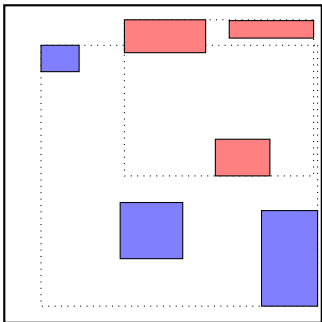
$$S = 20.71365$$

F C D E — B A



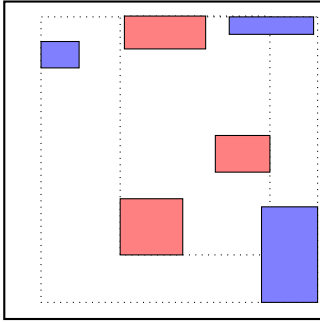
$$S = 17.795168$$

F C E — D B A



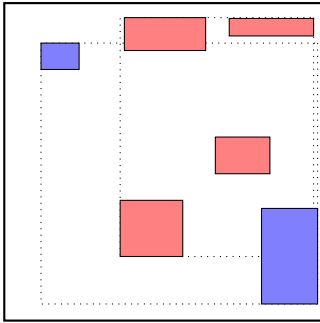
$$S = 17.795905$$

F D E — C B A



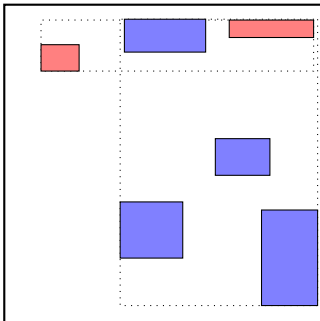
$S = 20.080004$

F E — D C B A



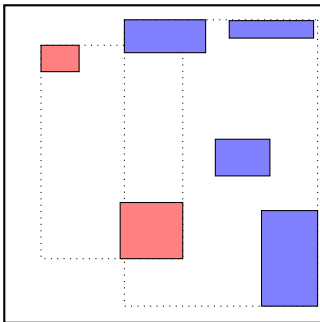
$S = 20.71365$

A B C E — D F



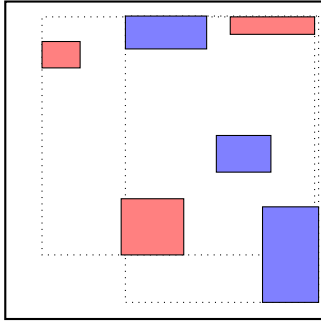
$S = 12.328305$

A B D E — C F



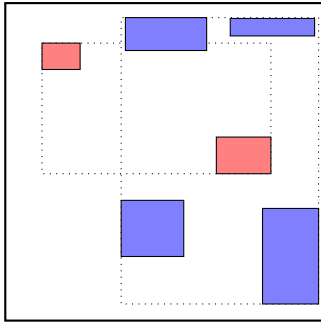
$S = 14.975254$

A B E — D C F



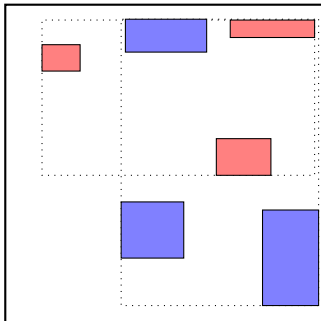
$$S = 21.037423$$

A C D E — B F



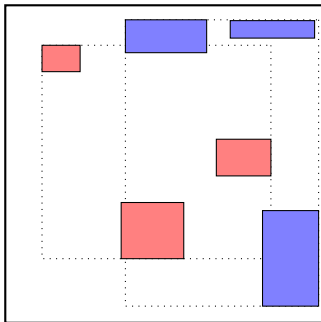
$$S = 15.12664$$

A C E — D B F



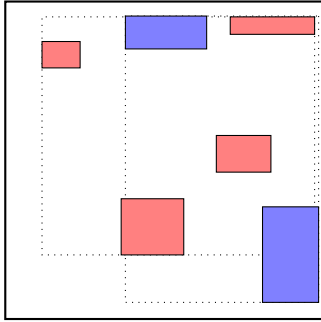
$$S = 17.30098$$

A D E — C B F



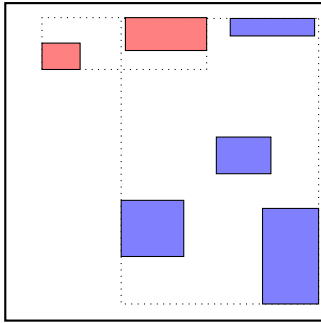
$$S = 18.230172$$

A E — D C B F



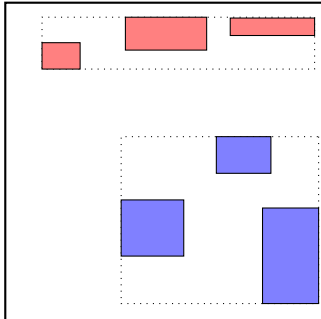
$$S = 21.037423$$

B C D E — A F



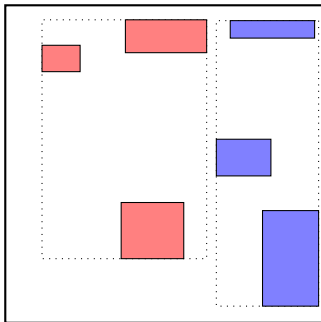
$$S = 11.3596325$$

B C E — D A F



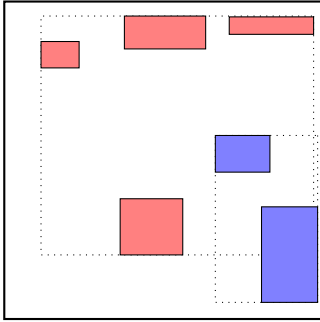
$$S = 8.241012$$

B D E — C A F



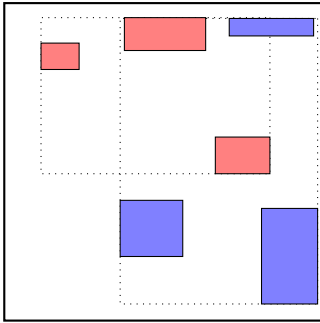
$$S = 11.992761$$

BE — D C A F



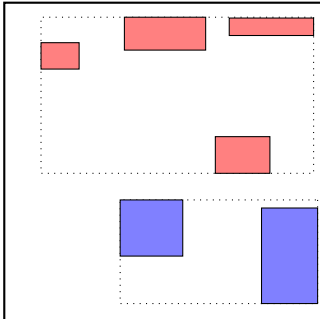
$$S = 14.382384$$

C D E — B A F



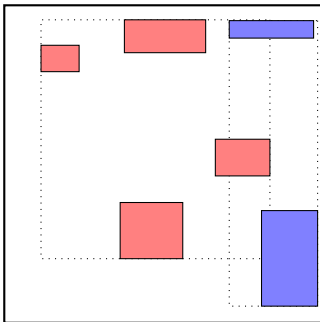
$$S = 16.118344$$

C E — D B A F



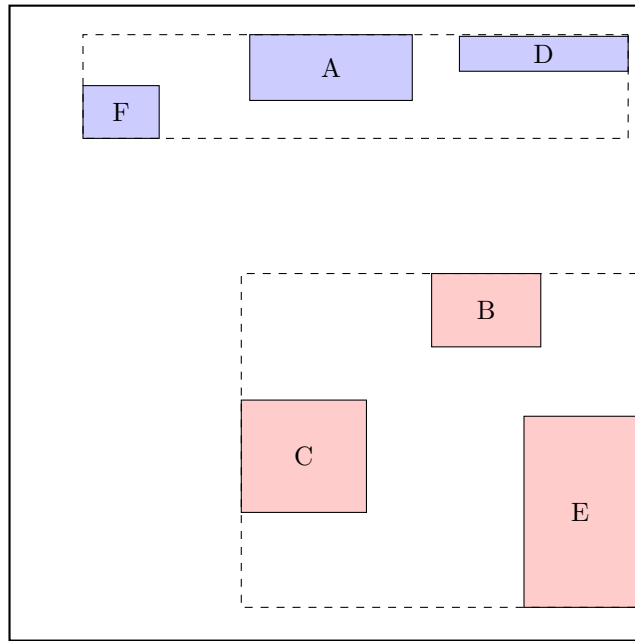
$$S = 11.027442$$

D E — C B A F



$$S = 13.983792$$

... the final split is:



return from SPLIT-NODE

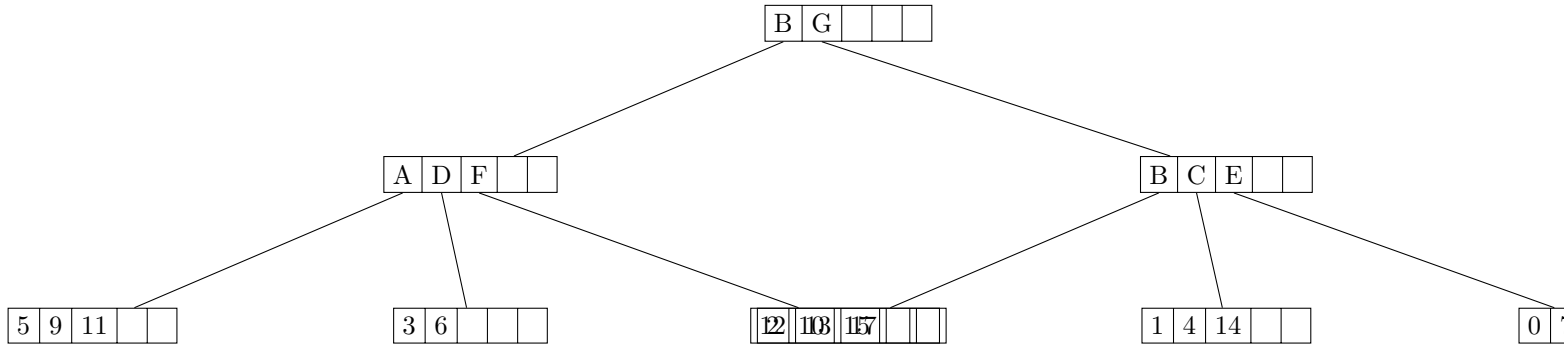
continue by adjusting the parent node NIL, the new parent

call ADJUST-TREE with R , node B and the new node

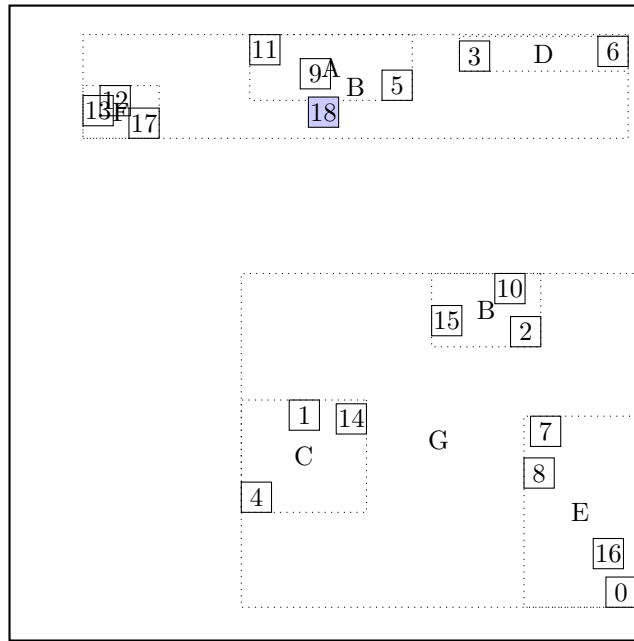
we are at the root

return from ADJUST-TREE

call INSERT *R*, #S(P :X 1977/1000 :Y 679/200)
 structure view:

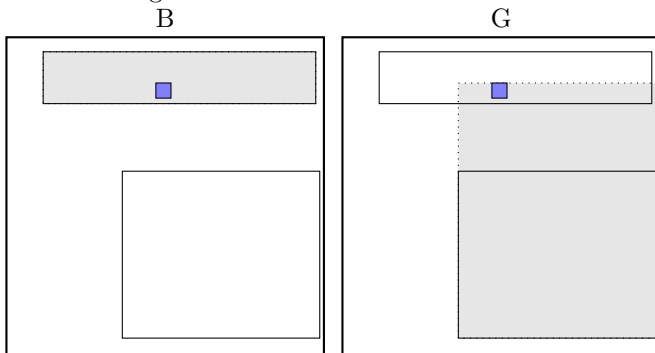


data view:



call CHOOSE-LEAF *R*, 18

choose among children:

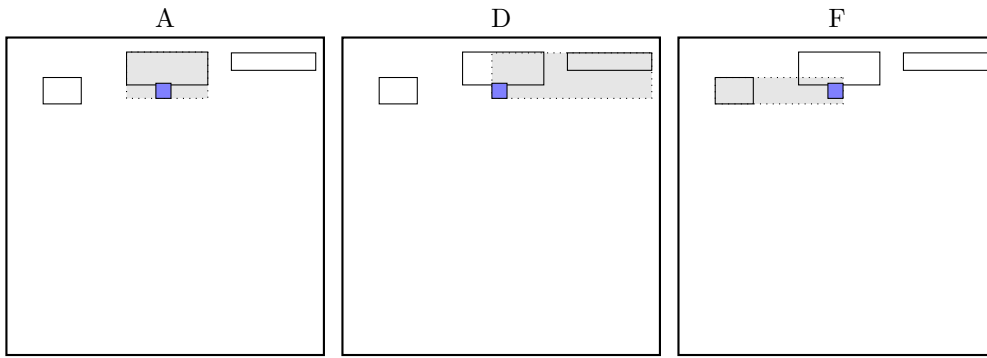


old area: 2.4737156
 new area: 2.4737156
 extension: 0.0

old area: 5.767296
 new area: 8.8155
 extension: 3.0482045

selected B

choose among children:



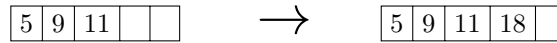
old area: 0.4676249
 new area: 0.6589749
 extension: 0.19134999

old area: 0.2577956
 new area: 1.2732294
 extension: 1.0154338

old area: 0.17589589
 new area: 0.5901585
 extension: 0.41426265

selected A
 a leaf is found: A
 return from CHOOSE-LEAF

the leaf A is not full, add the record.

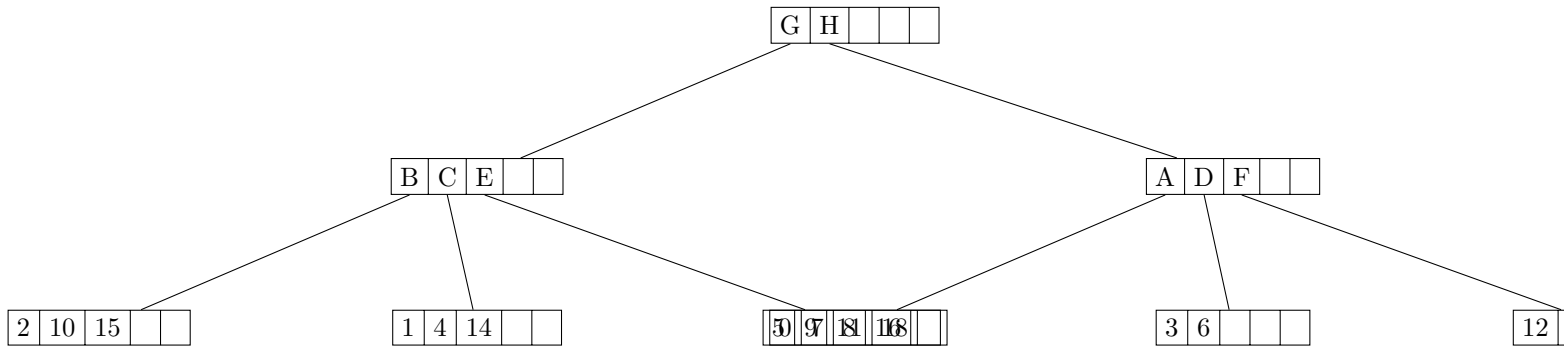


call ADJUST-TREE with R , node A
 update MBR of node A.
 continue by adjusting the parent node B

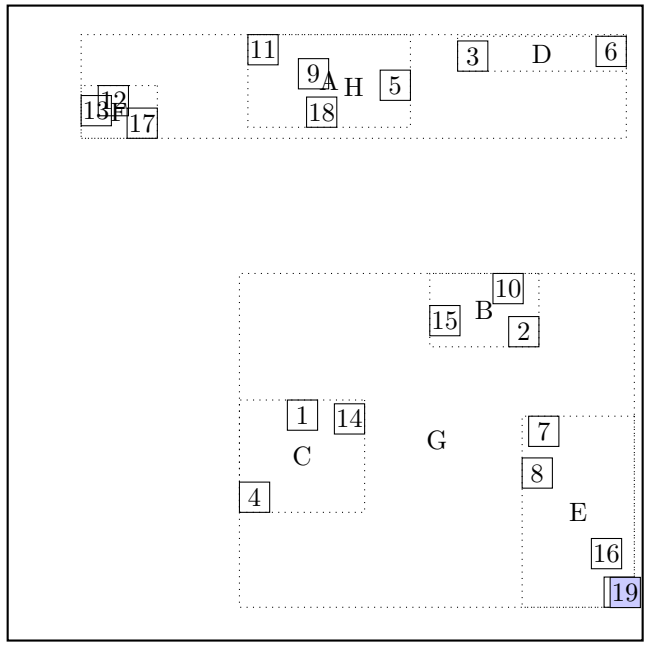
call ADJUST-TREE with R , node B
 update MBR of node B.
 continue by adjusting the parent node root

call ADJUST-TREE with R , node root
 we are at the root
 return from ADJUST-TREE

call INSERT *R*, #S(P :X 797/200 :Y 109/500)
 structure view:

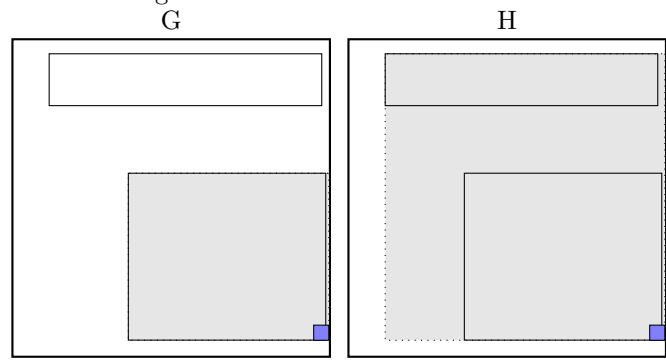


data view:



call CHOOSE-LEAF *R*, 19

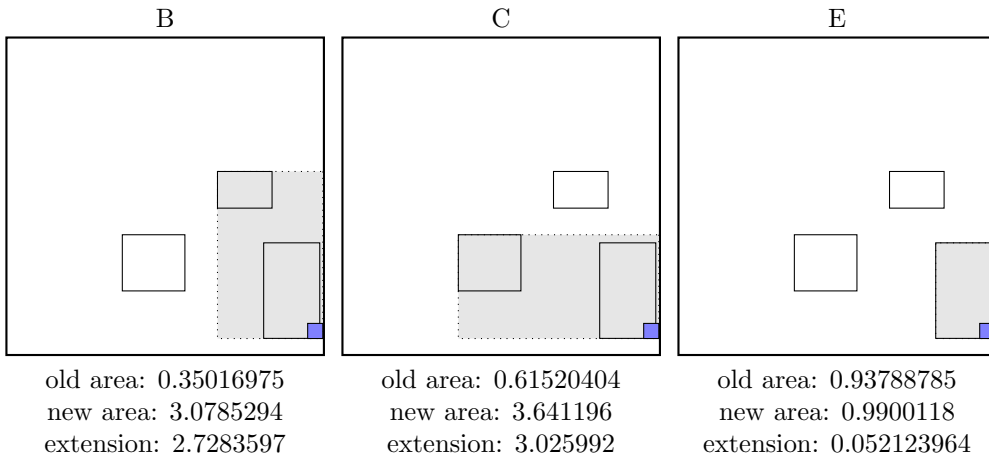
choose among children:



old area: 5.767296
 new area: 5.8609195
 extension: 0.09362364
 selected G

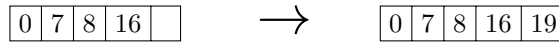
old area: 2.4737156
 new area: 14.01921
 extension: 11.545494

choose among children:



selected E
 a leaf is found: E
 return from CHOOSE-LEAF

the leaf E is not full, add the record.

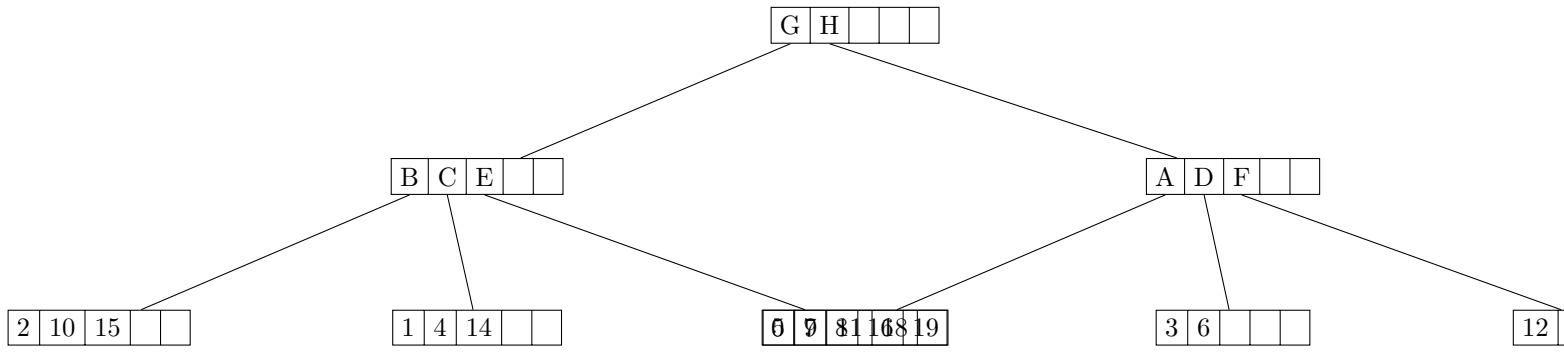


call ADJUST-TREE with R , node E
 update MBR of node E.
 continue by adjusting the parent node G

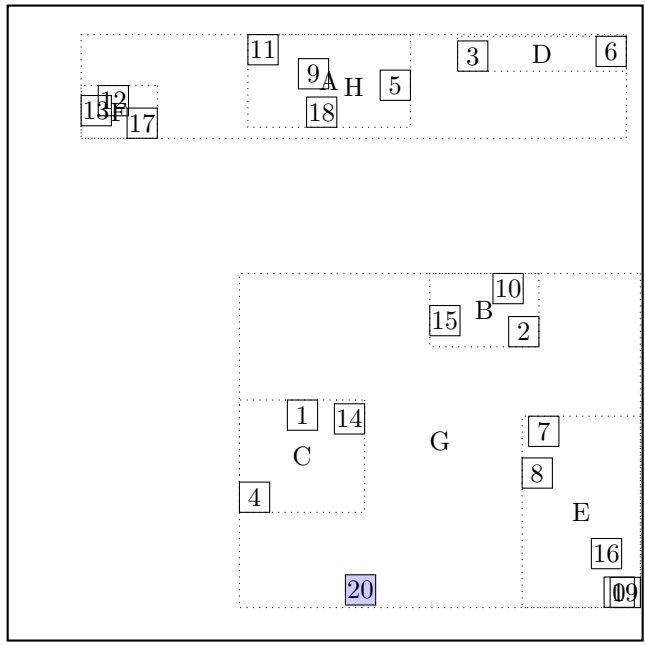
call ADJUST-TREE with R , node G
 update MBR of node G.
 continue by adjusting the parent node root

call ADJUST-TREE with R , node root
 we are at the root
 return from ADJUST-TREE

call INSERT *R*, #S(P :X 1117/500 :Y 47/200)
 structure view:

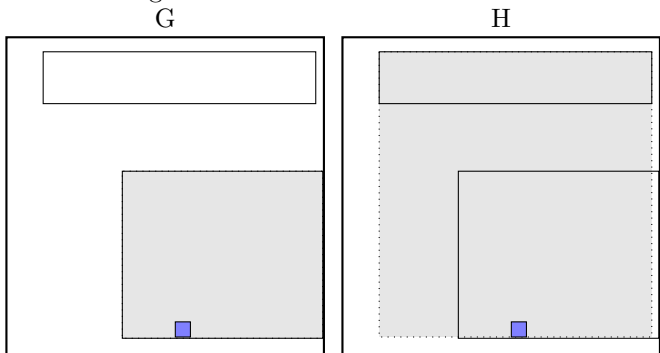


data view:



call CHOOSE-LEAF *R*, 20

choose among children:

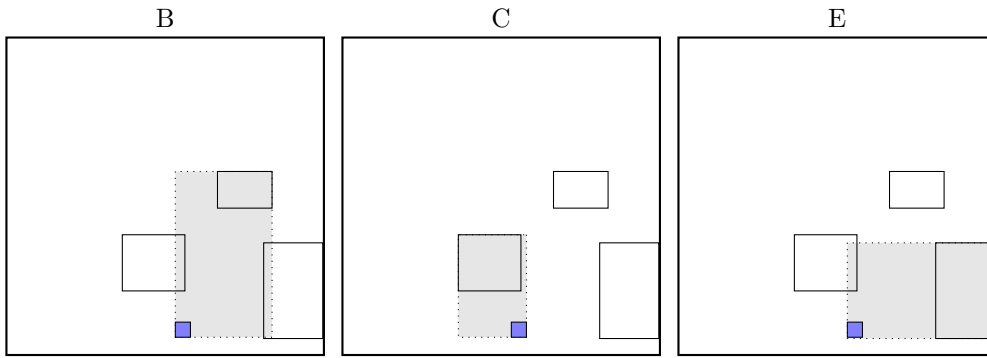


old area: 5.8609195
 new area: 5.8609195
 extension: 0.0

old area: 2.4737156
 new area: 13.605438
 extension: 11.131722

selected G

choose among children:



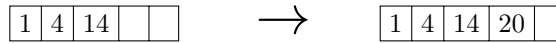
old area: 0.35016975
 new area: 2.8070393
 extension: 2.4568696

old area: 0.61520404
 new area: 1.221756
 extension: 0.60655195

old area: 0.9900118
 new area: 2.469966
 extension: 1.4799541

selected C
 a leaf is found: C
 return from CHOOSE-LEAF

the leaf C is not full, add the record.

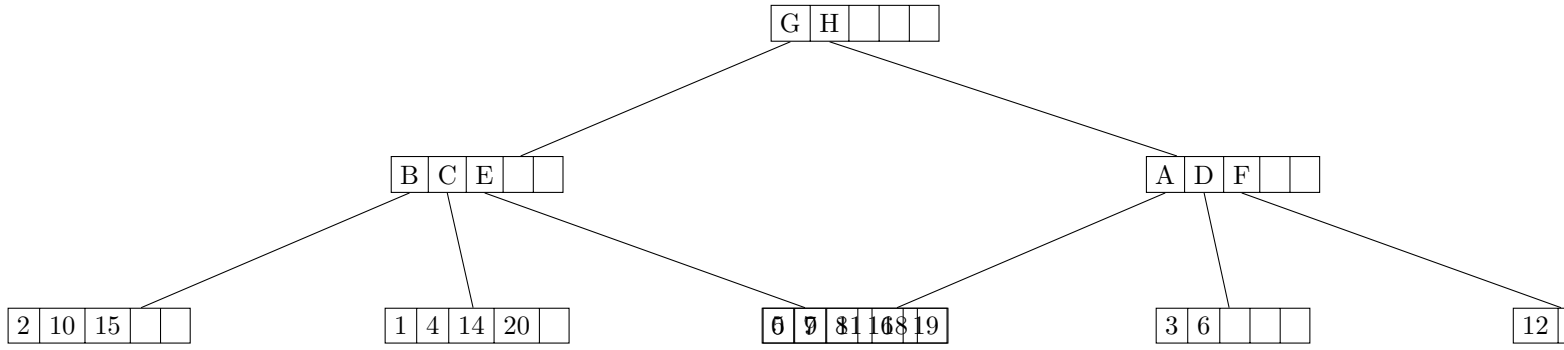


call ADJUST-TREE with R , node C
 update MBR of node C.
 continue by adjusting the parent node G

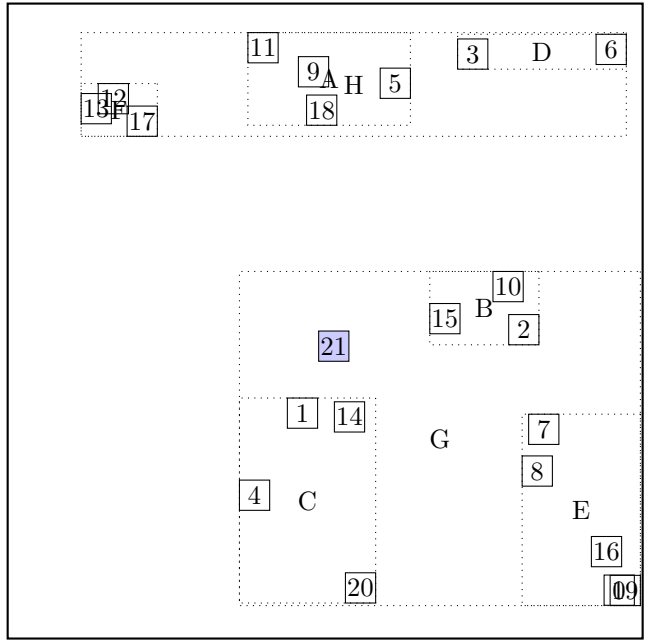
call ADJUST-TREE with R , node G
 update MBR of node G.
 continue by adjusting the parent node root

call ADJUST-TREE with R , node root
 we are at the root
 return from ADJUST-TREE

call INSERT R, #S(P :X 2057/1000 :Y 917/500)
 structure view:

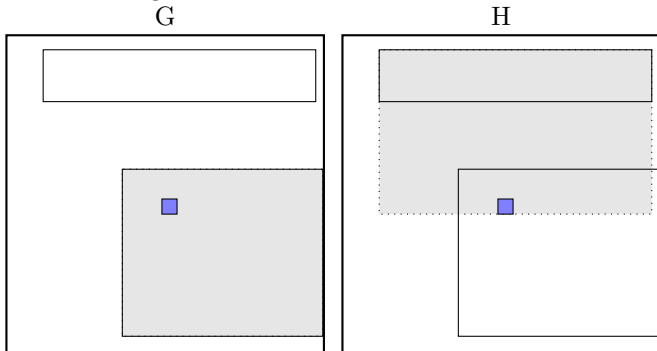


data view:



call CHOOSE-LEAF R, 21

choose among children:

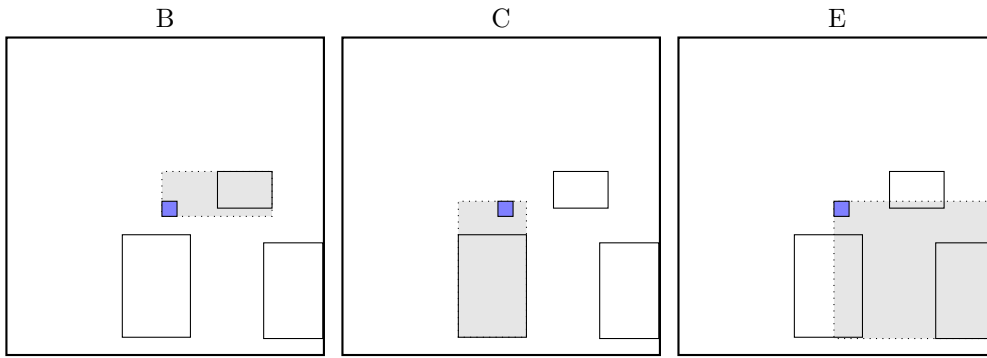


old area: 5.8609195
 new area: 5.8609195
 extension: 0.0

old area: 2.4737156
 new area: 7.839444
 extension: 5.3657284

selected G

choose among children:



old area: 0.35016975
 new area: 0.8654577
 extension: 0.515288

old area: 1.221756
 new area: 1.6208989
 extension: 0.39914286

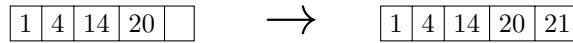
old area: 0.9900118
 new area: 3.8644486
 extension: 2.8744369

selected C

a leaf is found: C

return from CHOOSE-LEAF

the leaf C is not full, add the record.

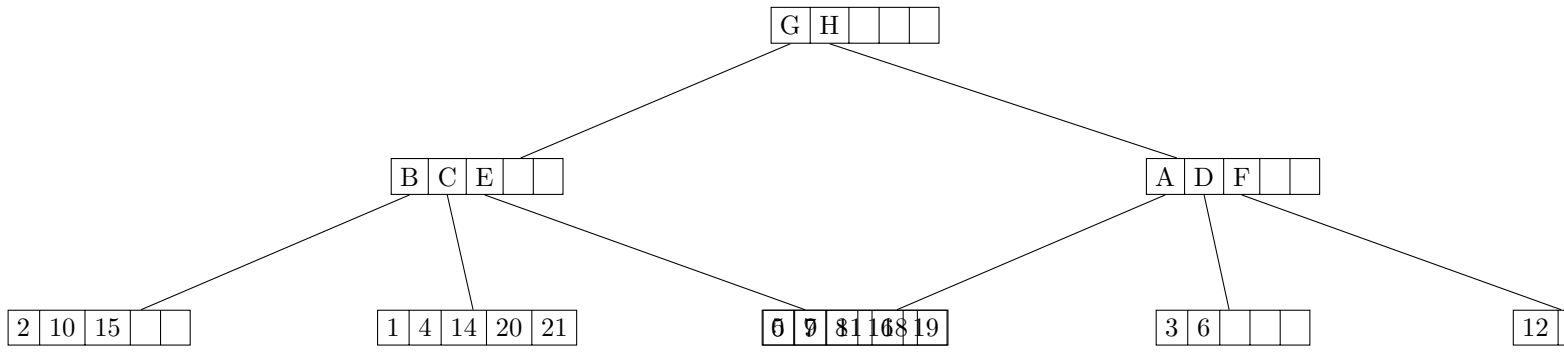


call ADJUST-TREE with R , node C
 update MBR of node C.
 continue by adjusting the parent node G

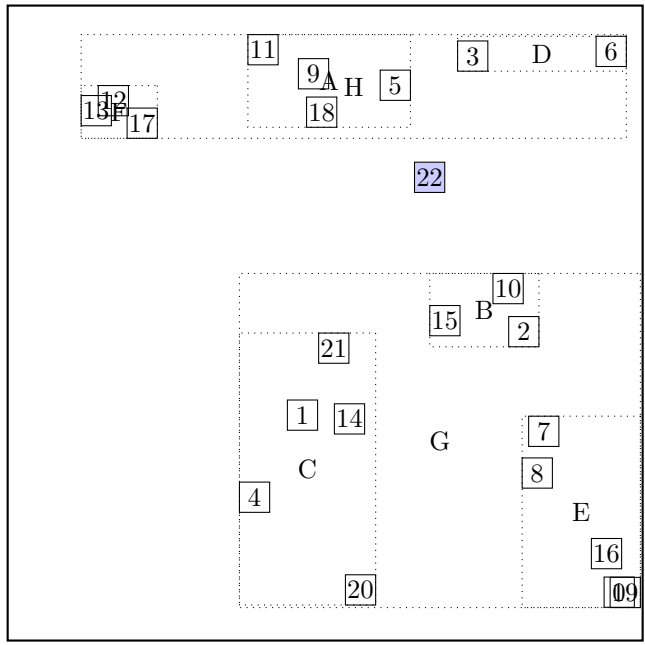
call ADJUST-TREE with R , node G
 update MBR of node G.
 continue by adjusting the parent node root

call ADJUST-TREE with R , node root
 we are at the root
 return from ADJUST-TREE

call INSERT R, #S(P :X 2691/1000 :Y 741/250)
 structure view:

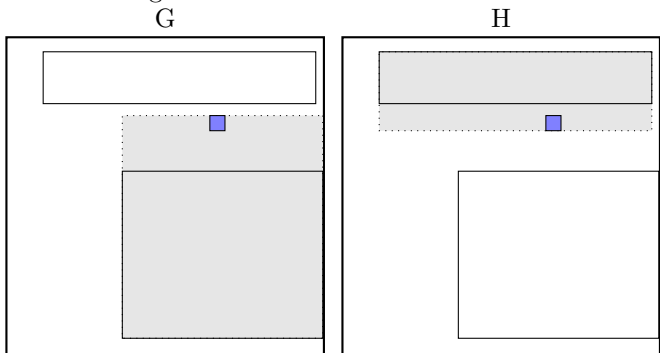


data view:



call CHOOSE-LEAF R, 22

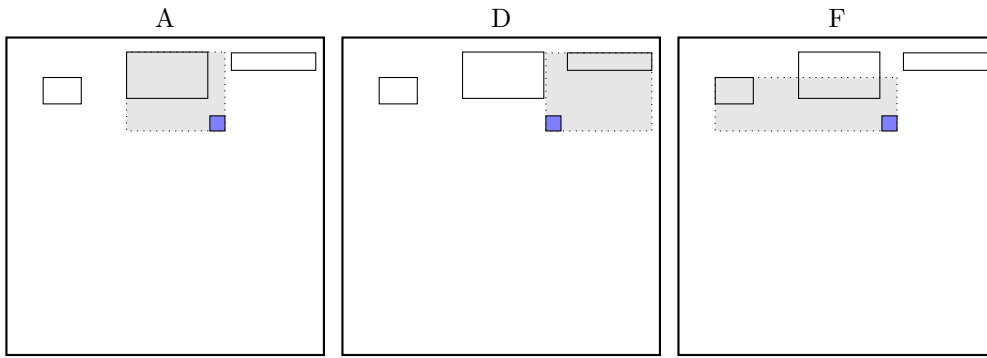
choose among children:



old area: 5.8609195
 new area: 7.8127914
 extension: 1.9518719

old area: 2.4737156
 new area: 3.7646637
 extension: 1.2909482

selected H
 choose among children:



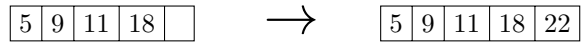
old area: 0.6589749
 new area: 1.3592879
 extension: 0.700313

old area: 0.2577956
 new area: 1.4472325
 extension: 1.1894369

old area: 0.17589589
 new area: 1.7003344
 extension: 1.5244385

selected A
 a leaf is found: A
 return from CHOOSE-LEAF

the leaf A is not full, add the record.

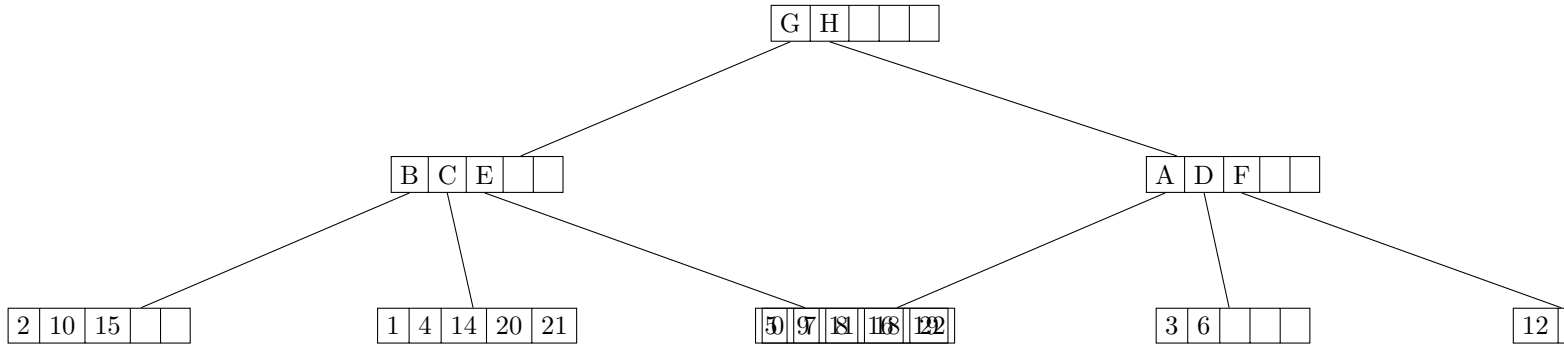


call ADJUST-TREE with R , node A
 update MBR of node A.
 continue by adjusting the parent node H

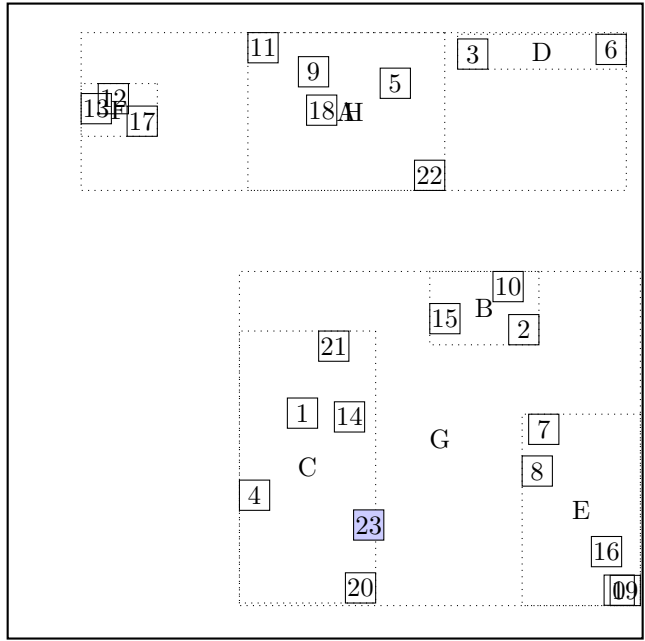
call ADJUST-TREE with R , node H
 update MBR of node H.
 continue by adjusting the parent node root

call ADJUST-TREE with R , node root
 we are at the root
 return from ADJUST-TREE

call INSERT *R*, #S(P :X 286/125 :Y 651/1000)
 structure view:

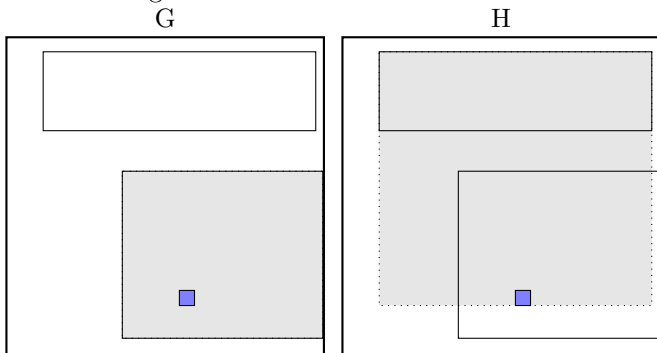


data view:



call CHOOSE-LEAF *R*, 23

choose among children:



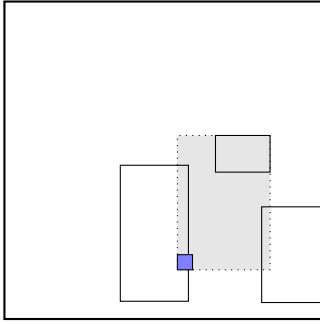
old area: 5.8609195
 new area: 5.8609195
 extension: 0.0

old area: 3.7646637
 new area: 12.105341
 extension: 8.340677

selected G

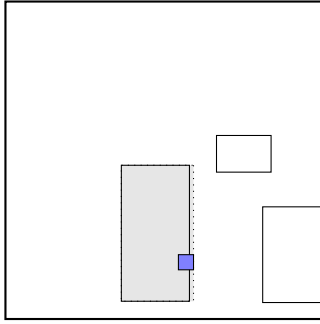
choose among children:

B



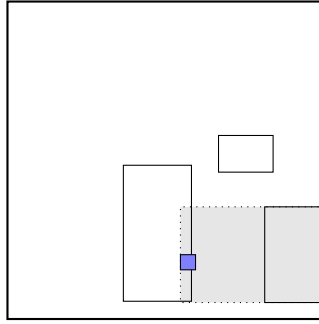
old area: 0.35016975
 new area: 2.178601
 extension: 1.8284313

C



old area: 1.6208989
 new area: 1.7180451
 extension: 0.09714627

E



old area: 0.9900118
 new area: 2.4016018
 extension: 1.41159

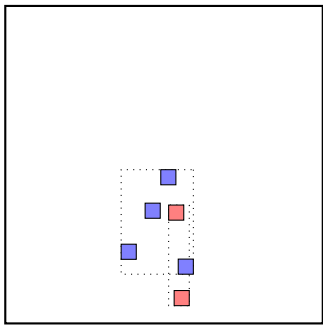
selected C

a leaf is found: C

return from CHOOSE-LEAF

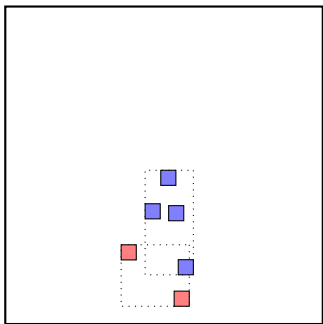
call SPLIT-NODE (bruteforce)

23 1 4 21 — 20 14



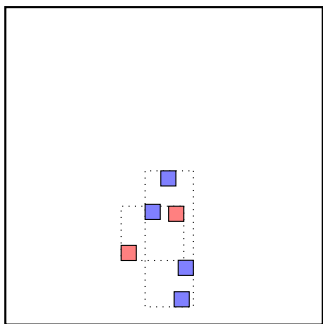
$S = 1.6841277$

23 1 14 21 — 20 4



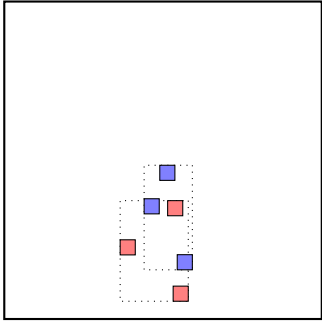
$S = 1.614867$

23 1 20 21 — 14 4



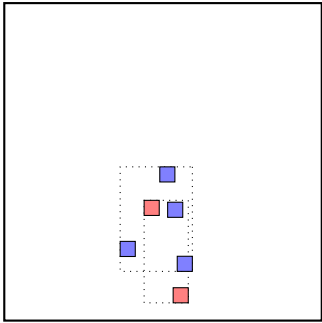
$S = 1.7422662$

23 1 21 — 20 14 4



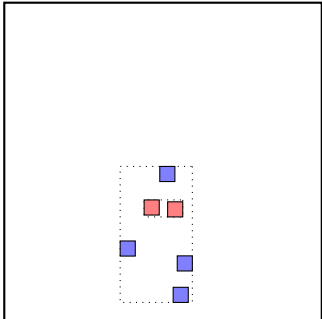
$$S = 2.081585$$

23 4 14 21 — 20 1



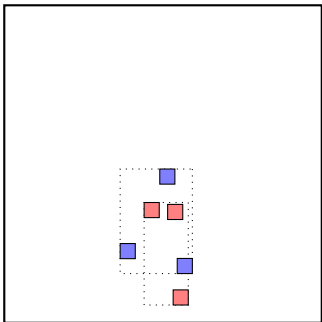
$$S = 2.112669$$

23 4 20 21 — 14 1



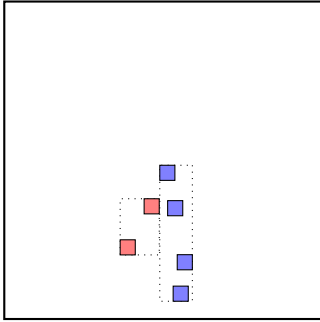
$$S = 1.8330201$$

23 4 21 — 20 14 1



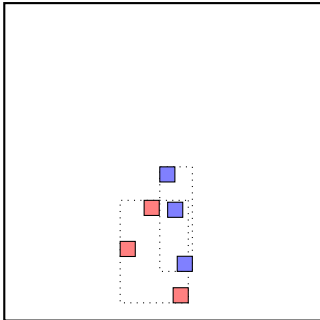
$$S = 2.112669$$

23 14 20 21 — 4 1



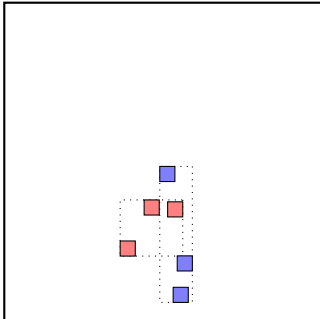
$$S = 1.1595004$$

23 14 21 — 20 4 1



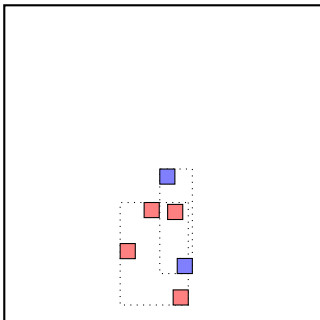
$$S = 1.8178291$$

23 20 21 — 14 4 1



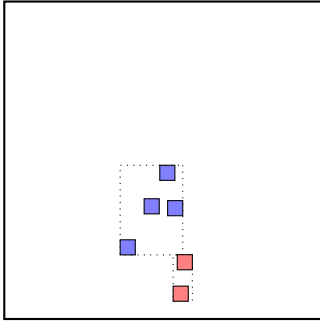
$$S = 1.3905733$$

23 21 — 20 14 4 1



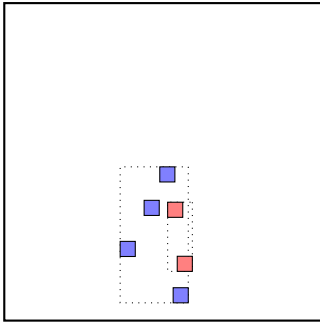
$$S = 1.8178291$$

1 4 14 21 — 20 23



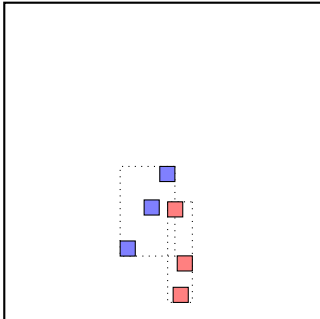
$$S = 1.1384721$$

1 4 20 21 — 14 23



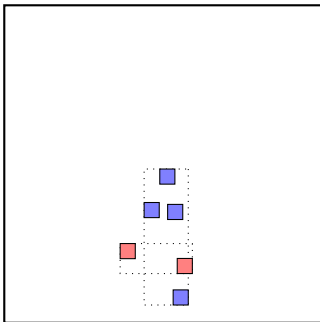
$$S = 1.9201038$$

1 4 21 — 20 14 23



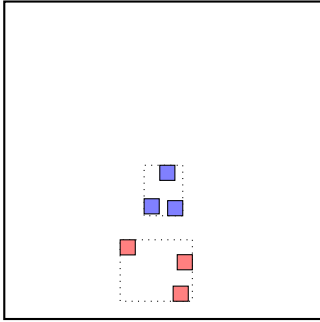
$$S = 1.2939009$$

1 14 20 21 — 4 23



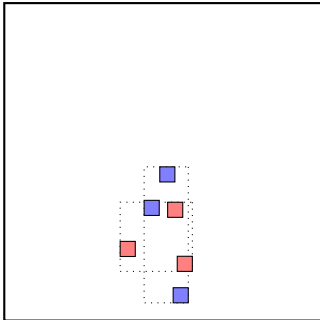
$$S = 1.4297508$$

1 14 21 — 20 4 23



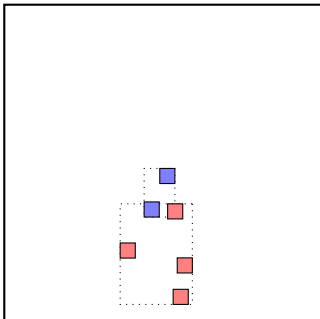
$$S = 1.117763$$

1 20 21 — 14 4 23



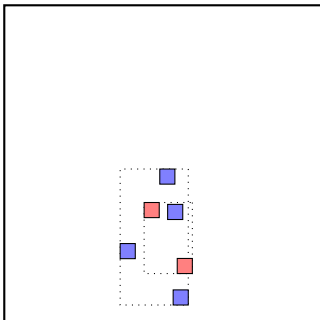
$$S = 1.9244409$$

1 21 — 20 14 4 23



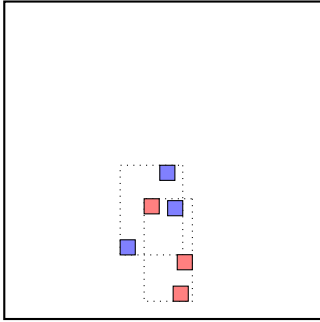
$$S = 1.532806$$

4 14 20 21 — 1 23



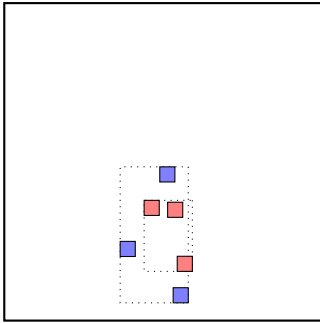
$$S = 2.220619$$

4 14 21 — 20 1 23



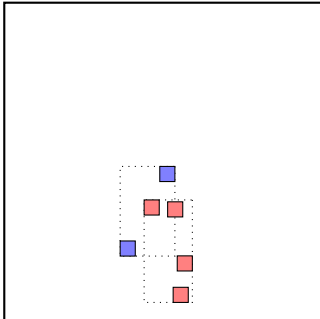
$S = 1.847136$

4 20 21 — 14 1 23



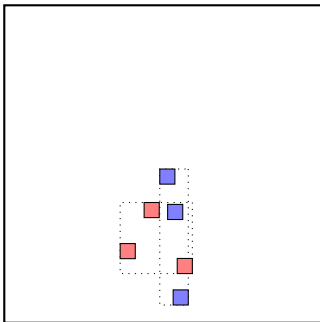
$S = 2.220619$

4 21 — 20 14 1 23



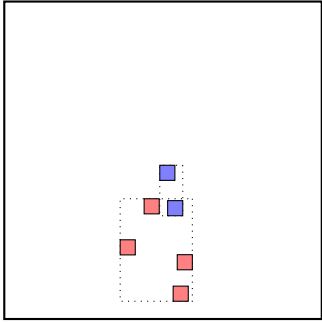
$S = 1.723792$

14 20 21 — 4 1 23



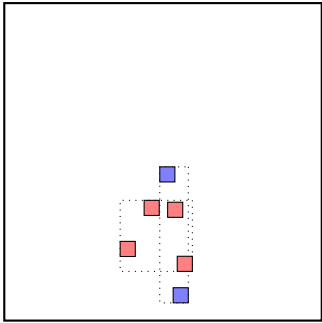
$S = 1.575923$

14 21 — 20 4 1 23



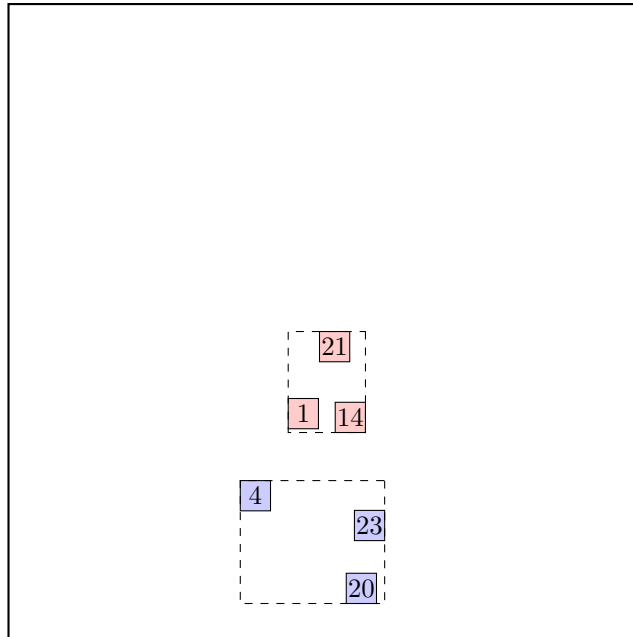
$S = 1.4980521$

20 21 — 14 4 1 23



$S = 1.575923$

... the final split is:



return from SPLIT-NODE

call ADJUST-TREE with R , node C and the new node
 update MBR of node C.
 add the new node to the parent node G

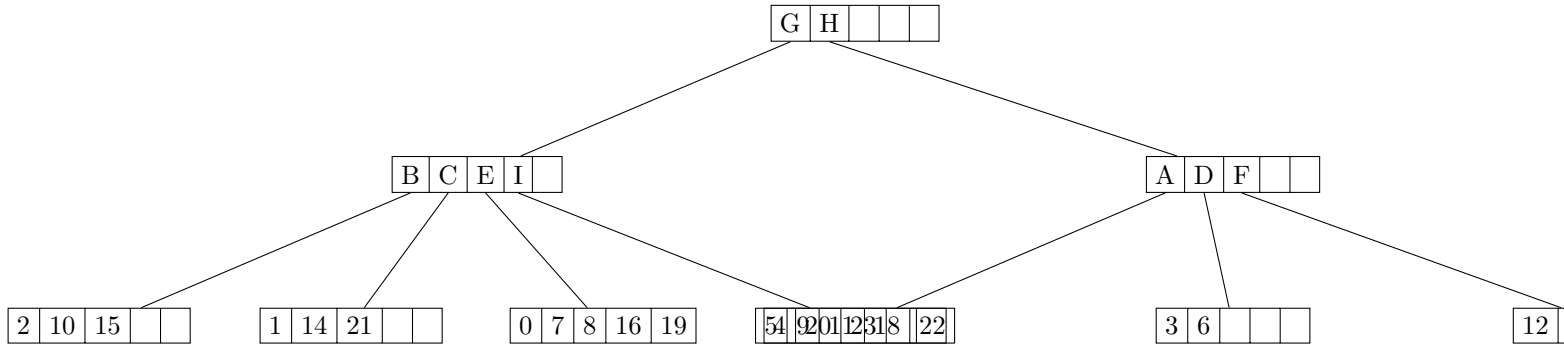
call ADJUST-TREE with R , node G
 update MBR of node G.
 continue by adjusting the parent node root

call ADJUST-TREE with R , node root

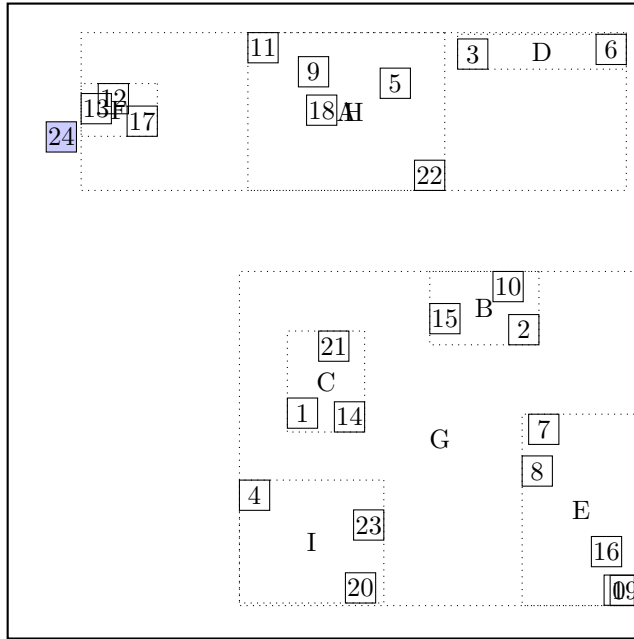
we are at the root
return from ADJUST-TREE

call INSERT *R*, #S(P :X 51/200 :Y 1609/500)

structure view:

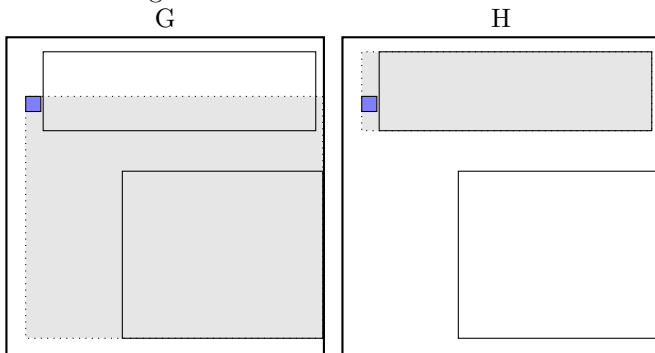


data view:



call CHOOSE-LEAF *R*, 24

choose among children:

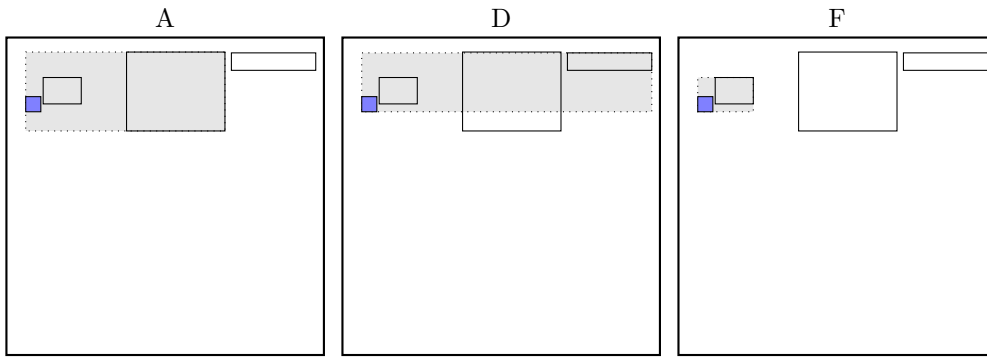


old area: 5.8609195
new area: 12.575999
extension: 6.71508

old area: 3.7646637
new area: 4.0058274
extension: 0.24116373

selected H

choose among children:



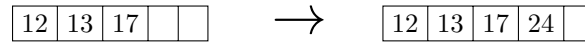
old area: 1.3592879
 new area: 2.7519837
 extension: 1.3926958

old area: 0.2577956
 new area: 2.9890223
 extension: 2.7312267

old area: 0.17589589
 new area: 0.33295488
 extension: 0.157059

selected F
 a leaf is found: F
 return from CHOOSE-LEAF

the leaf F is not full, add the record.



call ADJUST-TREE with R , node F
 update MBR of node F.
 continue by adjusting the parent node H

call ADJUST-TREE with R , node H
 update MBR of node H.
 continue by adjusting the parent node root

call ADJUST-TREE with R , node root
 we are at the root
 return from ADJUST-TREE

